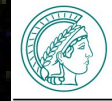
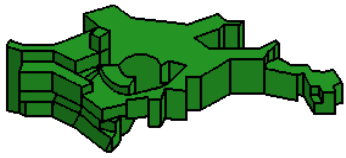


Max-Planck-Institut  
für Astrophysik



TUM



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O

LMU

Excellence Cluster  
Universe

Lectures, INAF-Osservatorio Astronomico di Brera  
19. & 20. November 2013

# The Violent Deaths of Massive Stars

## Diverse Routes to Stellar Death

### From Stellar Collapse to Explosion

Hans-Thomas Janka

(Max-Planck-Institut für Astrophysik, Garching, Germany)

# Contents

## Lecture I:

- Supernovae: classification and phenomenology
- Basics of stellar evolution & death scenarios in overview
- White dwarfs and thermonuclear supernovae

## Lecture II:

- Gravitational (core-collapse) supernovae: evolution stages
- SN modeling: some technical aspects
- Status of 2D and 3D SN modeling

## Lecture III:

- Supernova models: Predictions of observable signals
- Neutron stars: birth and death
- Black holes and gamma-ray bursts: Sources of heavy elements

For concise reviews of much of what I will say, see

**ARNPS 62 (2012) 407, arXiv:1206.2503**

and

**PTEP 2012, 01A309, arXiv:1211.1378**



# Explosion Mechanisms of Core-Collapse Supernovae

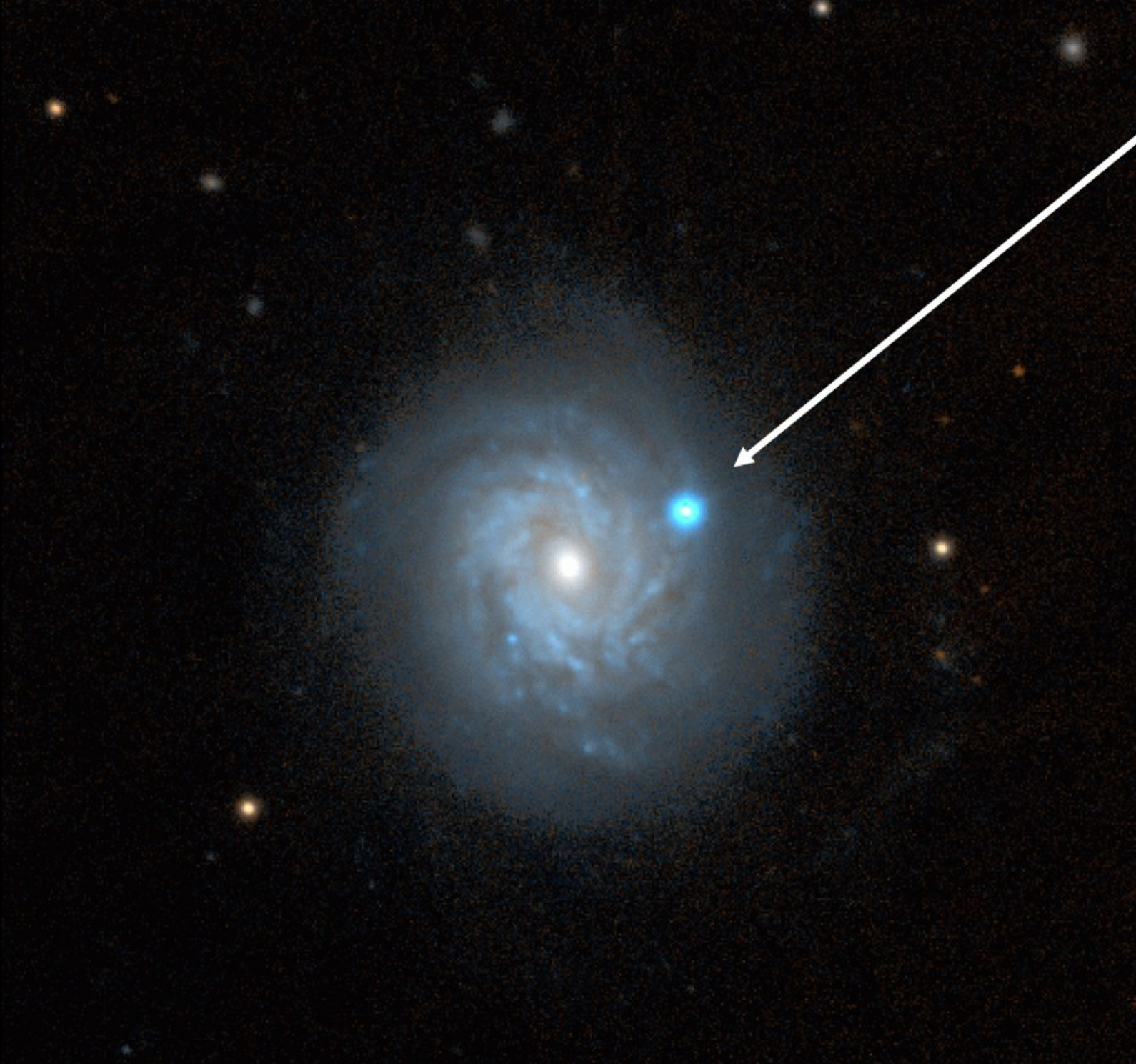
Hans-Thomas Janka

Max Planck Institute for Astrophysics, D-85748 Garching, Germany;  
email: thj@mpa-garching.mpg.de

# Supernova Phenomenology and Classification

SN 1994d



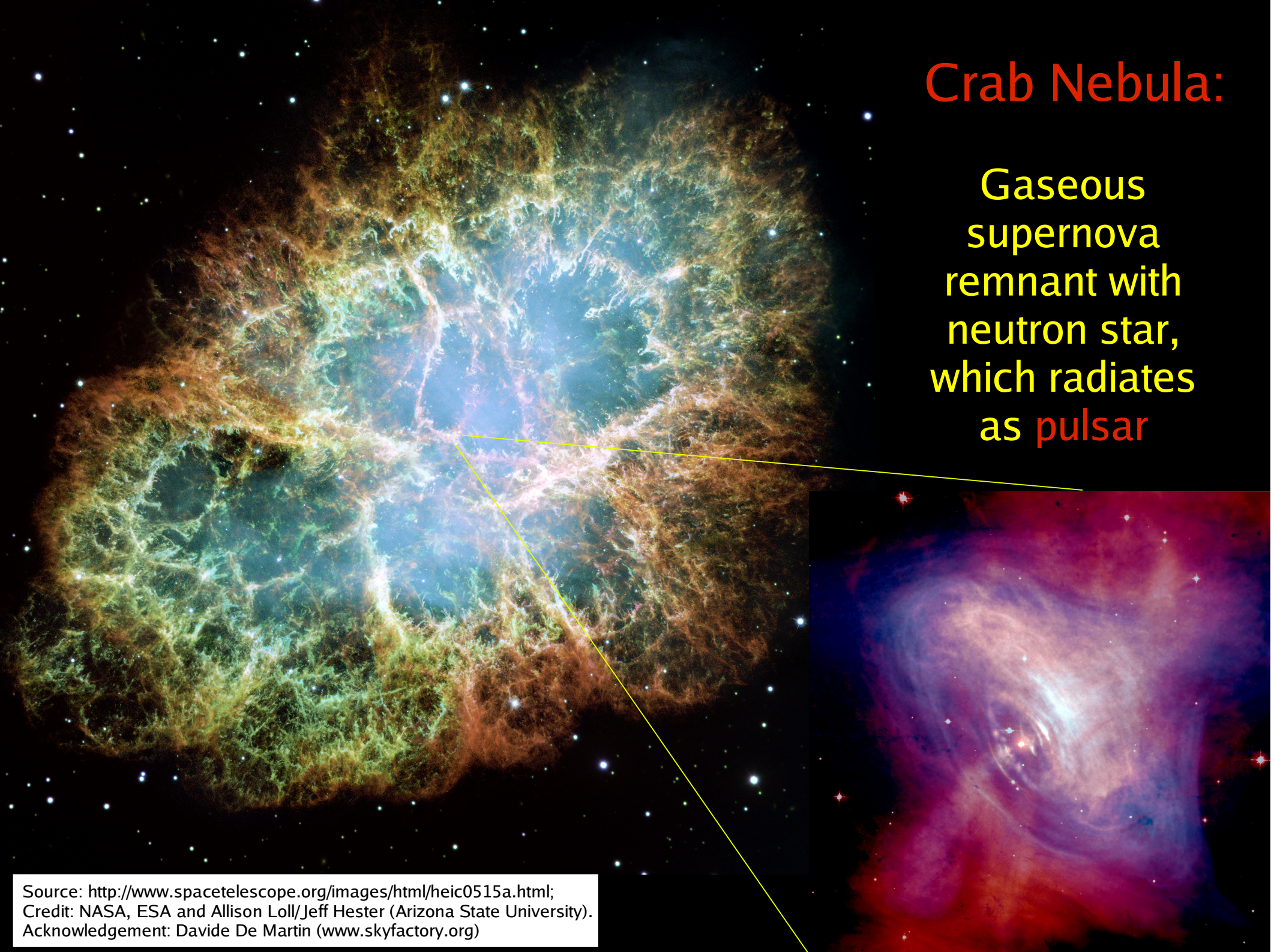


Source: [http://folk.uio.no/hdahle/Recent\\_SN.html](http://folk.uio.no/hdahle/Recent_SN.html)

NGC3982

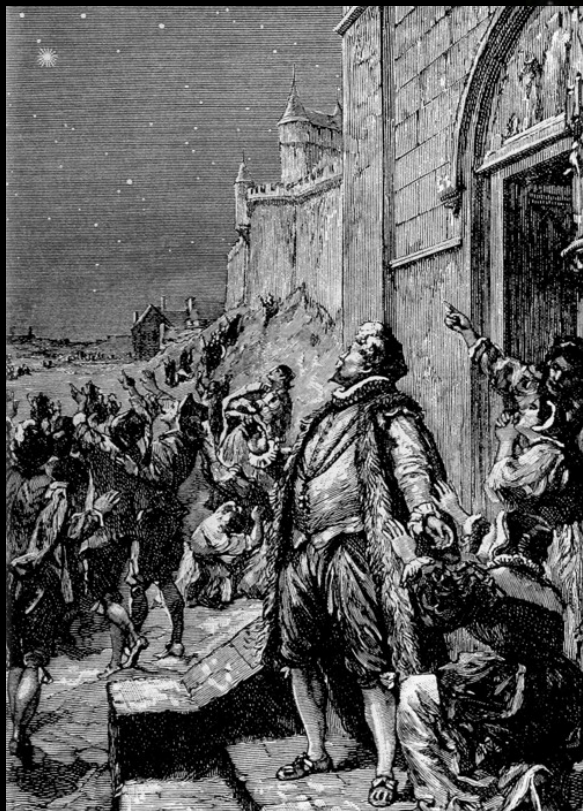
# Crab Nebula:

Gaseous  
supernova  
remnant with  
neutron star,  
which radiates  
as **pulsar**



Source: <http://www.spacetelescope.org/images/html/heic0515a.html>;  
Credit: NASA, ESA and Allison Loll/Jeff Hester (Arizona State University).  
Acknowledgement: Davide De Martin ([www.skyfactory.org](http://www.skyfactory.org))

# Tycho SNR



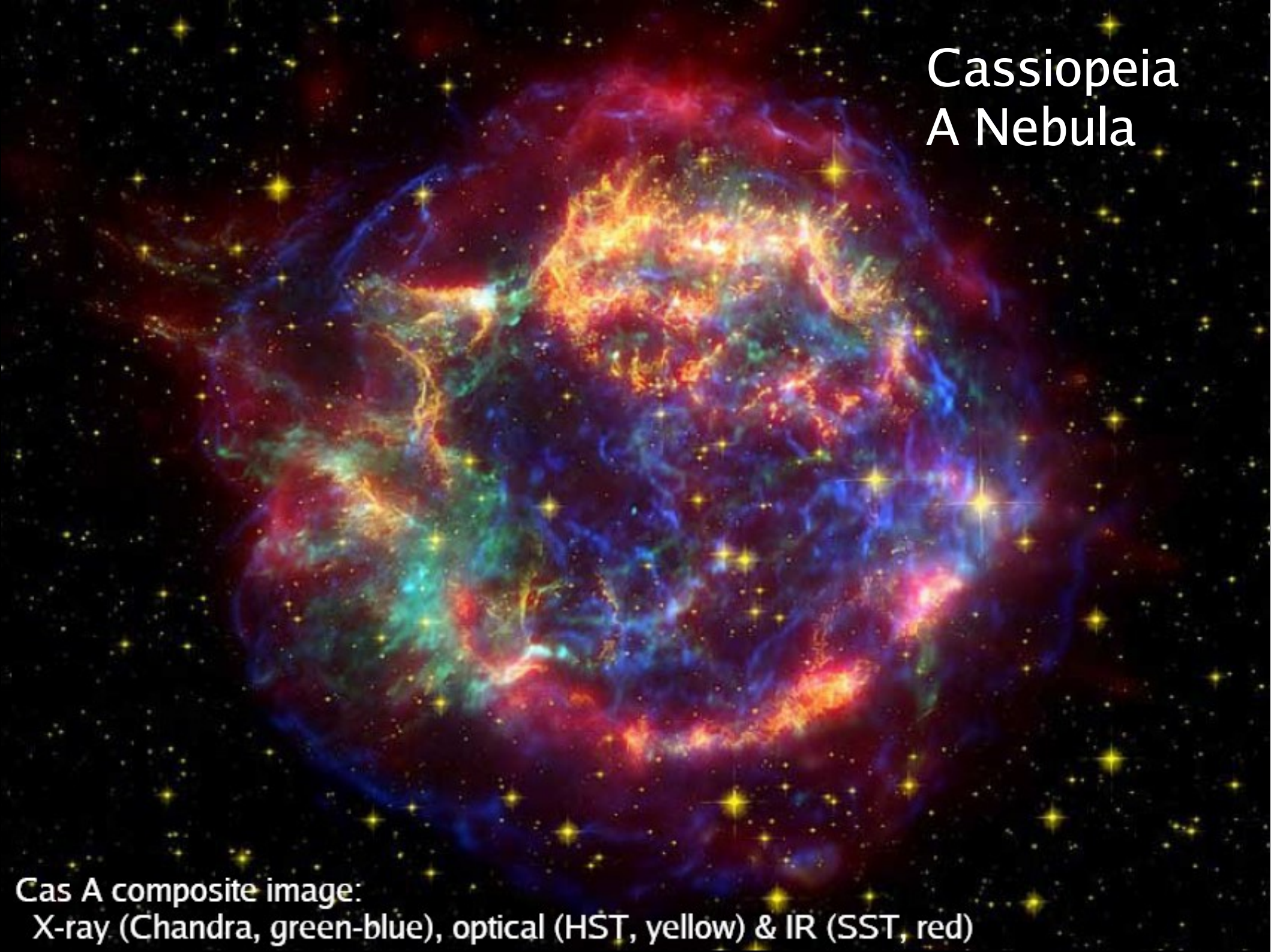
1572: Tycho Brahe  
observes "new star" that  
remains visible for months



(CHANDRA satellite image)



# Cassiopeia A Nebula



Cas A composite image:  
X-ray (Chandra, green-blue), optical (HST, yellow) & IR (SST, red)

# Supernovae in the Universe

- 1–10 supernovae explode in the Universe every second
- ~2 per 100 years in the Milky Way (historical records of ~10 past events, several with visible remnants)
- Several 100 distant supernovae observed every year in surveys
- Energy release in radiation:  $10^{49}$  erg  
Release of kinetic energy of ejected gas:  $10^{51}$  erg  
(1 erg =  $10^{-7}$  J;  $10^{51}$  erg = 1 bethe)
- Hypernovae and gamma-ray bursts (GRBs) can release up to 100 times more energy, but occur only in < 1% of all core collapses!

# Historically Reported Supernovae in the Milky Way Within the Past 1000 Years

**Tabelle 1.1** Bekannte Supernovaereignisse in unserer Milchstraße in den vergangenen 1000 Jahren. Bei den Supernovae von 1572 und 1680 konnte der Typ von Sternexplosion (siehe Kapitel 1.2) anhand von „Lichtechos“ mit moderner Technik kürzlich bestätigt werden. Astronomen gelang es, Strahlung des Explosionsblitzes aufzufangen, die von Gas- und Staubwolken in der Umgebung des zerstörten Sterns zurückgeworfen wurde. Die Reflexe waren aufgrund ihres Umwegs einige hundert Jahre länger zur Erde unterwegs als das direkte Licht der Supernova.

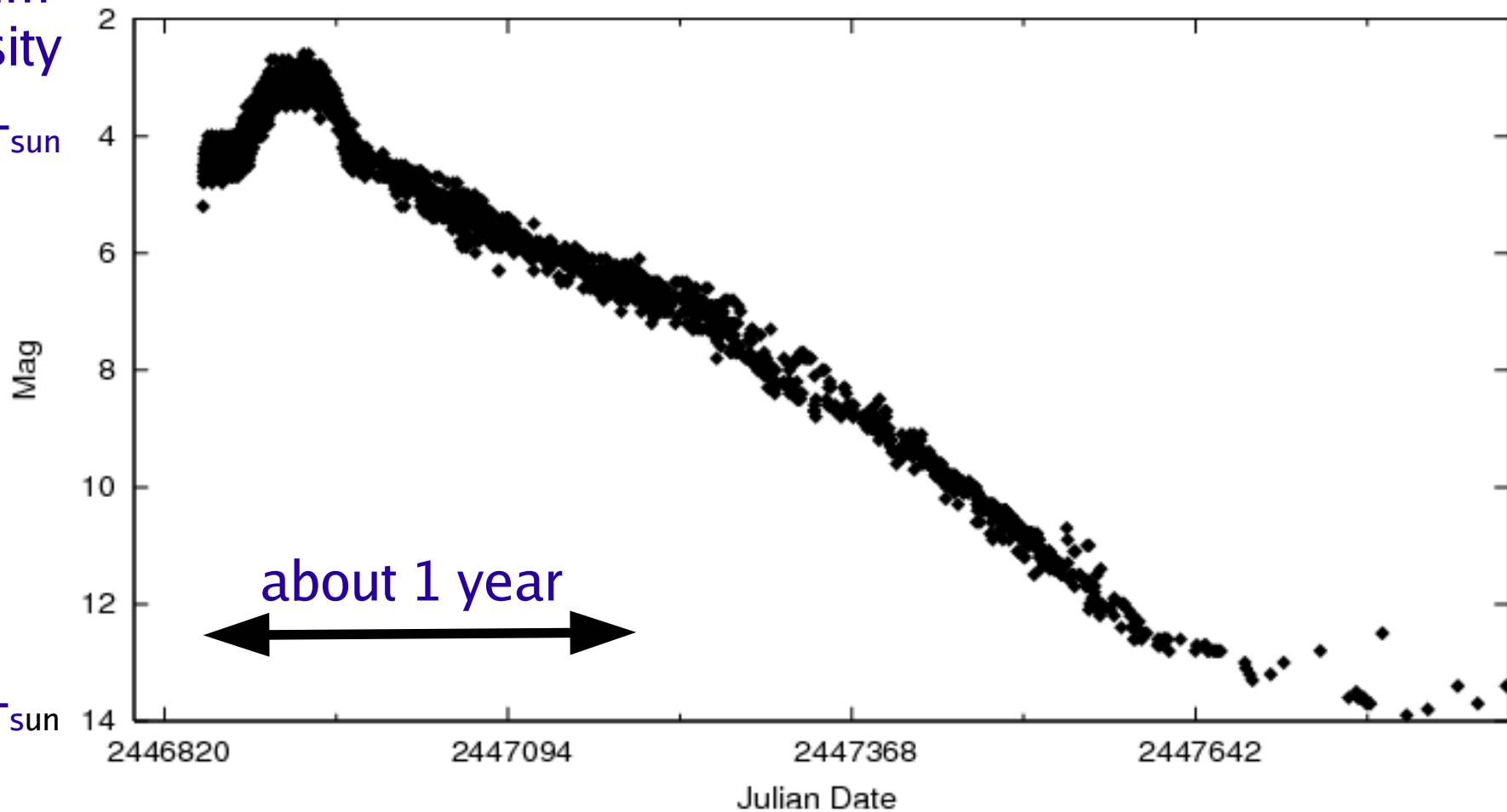
Jahr	Sichtbarkeitsdauer	Entfernung [Lichtjahre]	Beobachtungen (Ort/Astronom)	Typ	Überrest
1006	einige Jahre	7200	China, Japan, Arabien, Schweiz	SN Ia	Gasschale (Abbildung 4.1)
1054	ca. zwei Jahre	6500	China, Arabien	SN II	Krebsnebel und -pulsar (Abbildung 2.11)
1181	sechs Monate	>26 000	China, Japan	Kernkollaps?	Röntgen- und Radiopulsar J0205+6449 (3C 58); Assoziation mit SN 1181 unsicher
~1300	sechs Monate	~1500	Simbabwe	Kernkollaps?	Vela Junior; Gasschale (Röntgenquelle RX J0852.0-4622)
1572	16 Monate	7500	Tycho Brahe	SN Ia	Gasnebel (Abbildung 4.2)
1604	18 Monate	20 000	Johannes Kepler	SN Ia	Gasschale
~1680	?	11 000	John Flamsteed?	SN IIb	Kassiopeia A (Abbildung 1.1); Gasschale mit kompakter Röntgenquelle
~1870	unsichtbar durch Staub	25 000	–	?	Radio- und Röntgenquelle G1.9+0.3 (Abbildung 1.2)



# Supernova 1987A: Light Curve

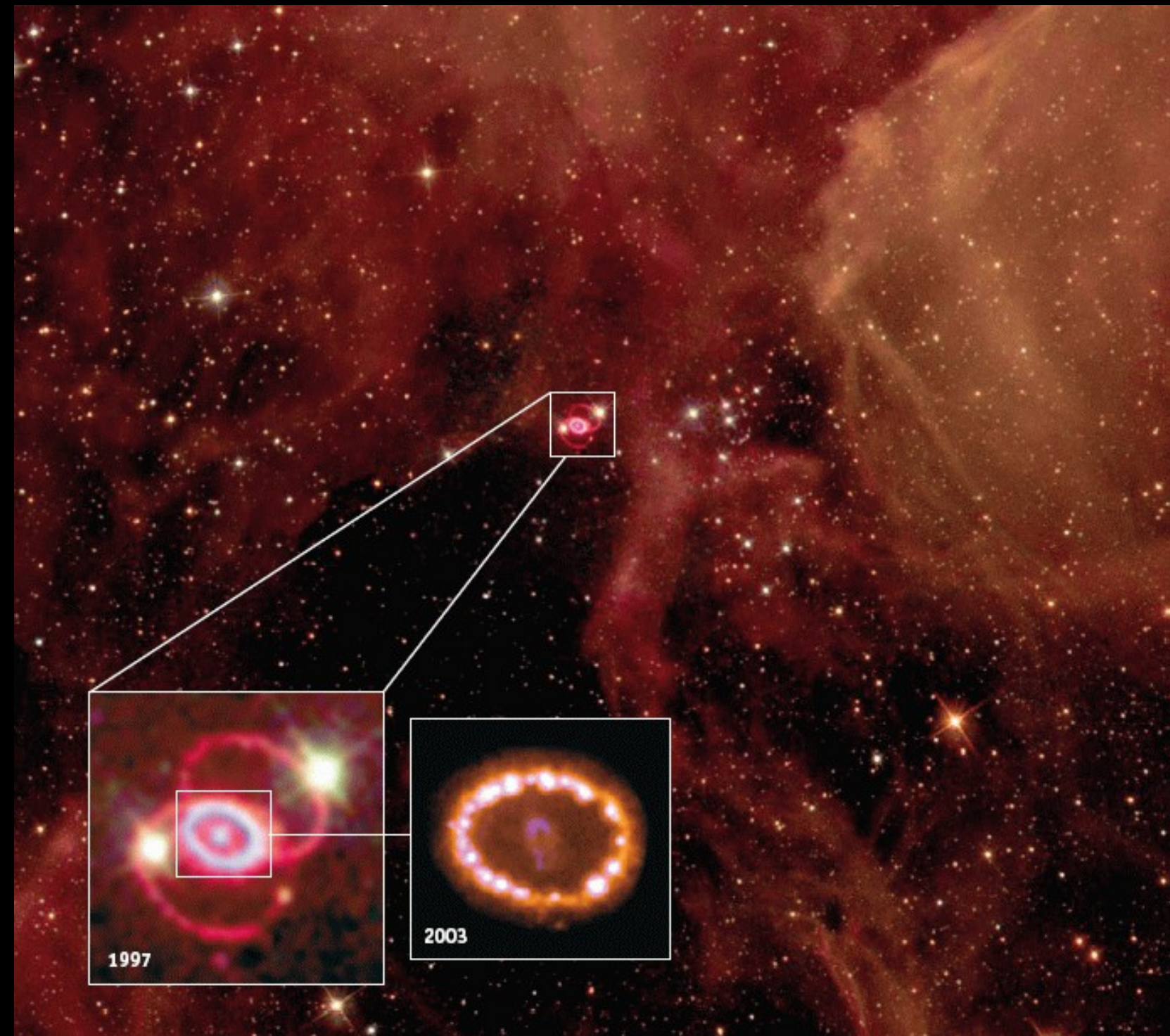
AAVSO DATA FOR SN 1987A - WWW.AAVSO.ORG

Maximum  
Luminosity  
 $\sim 2 \cdot 10^8 L_{\text{sun}}$



$\sim 10^4 L_{\text{sun}}$

Visual Validated ◆



Supernova  
1987A  
as a  
teenager

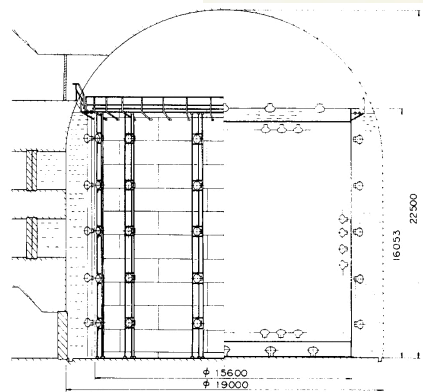
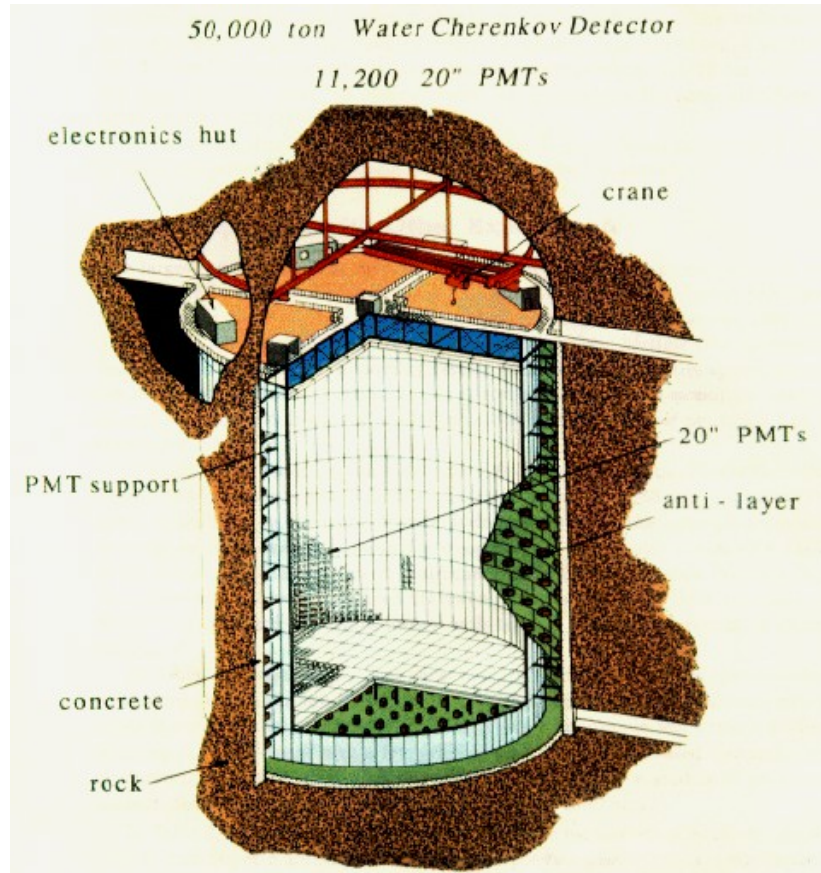
1997

2003

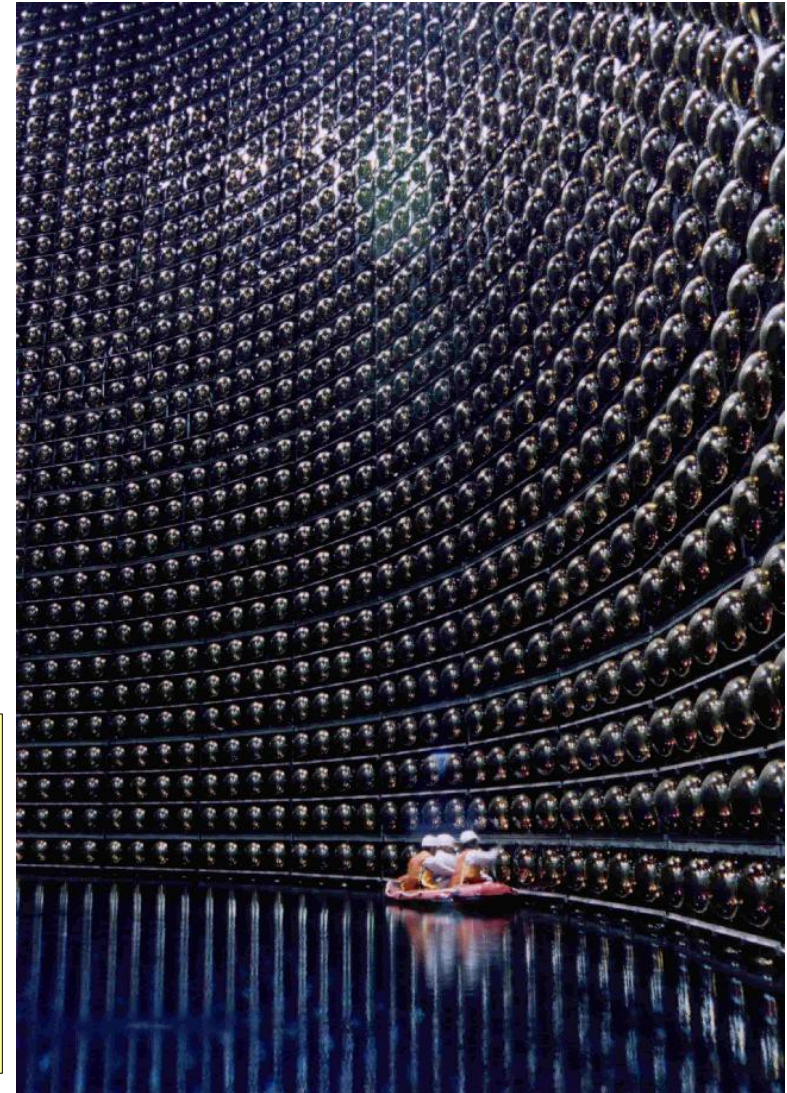
# Supernova 1987A

- Birthday: Februar 23rd, 1987
- Birth place: Large Magellanic Cloud
- Distance: about 170,000 lightyears
- Origin: blue supergiant star with about 20 solar masses
- Importance:
  - \* only nearby supernova in the past 400 years that was visible to the naked eye
  - \* unprecedented wealth of observational data
  - \* first measurement of extragalactic **neutrinos**
  - \* confirmation of neutron star birth theory
  - \* unambiguous information about **strongly turbulent processes** during stellar explosions

# Supernova 1987A

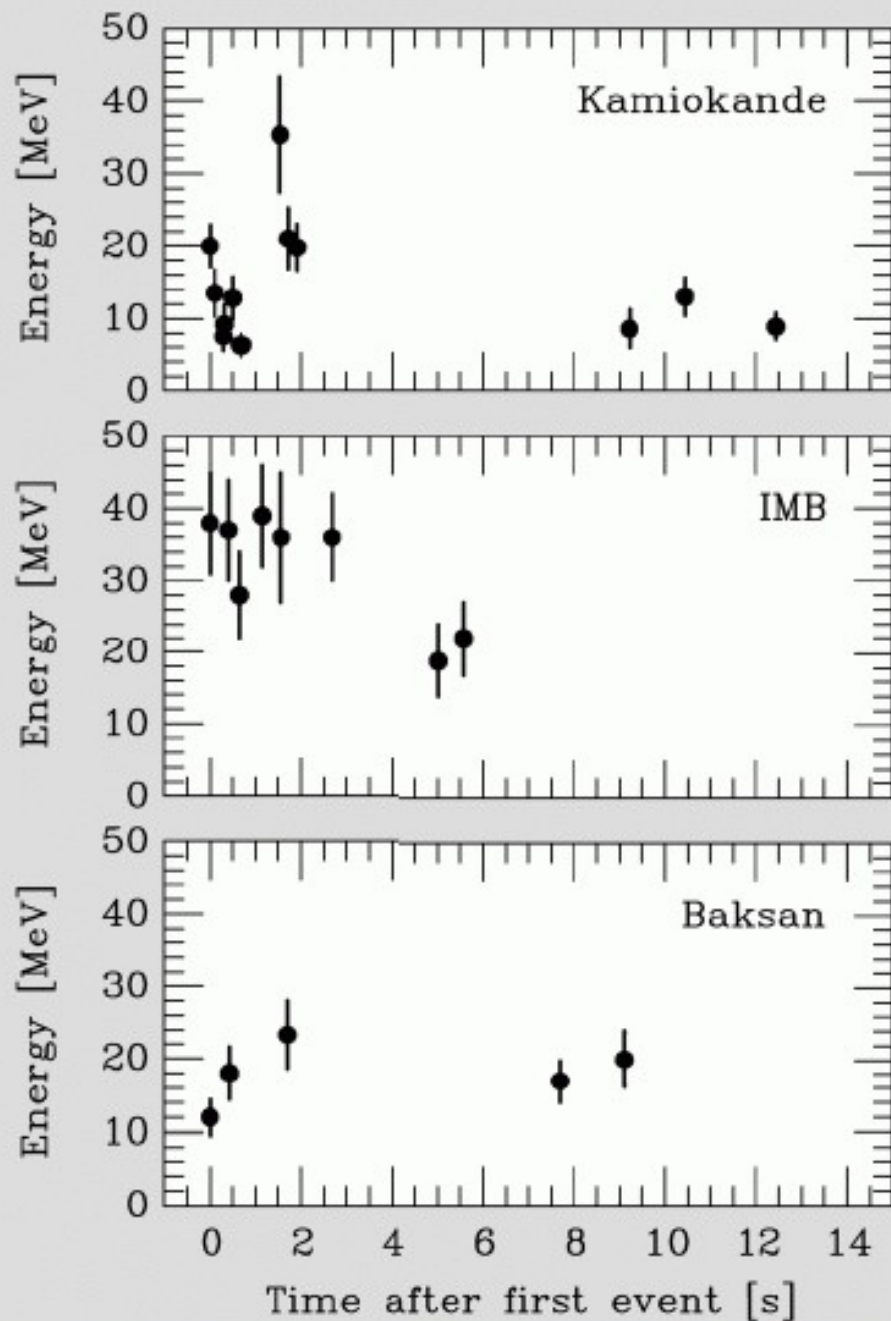


Two dozen (of  $10^{58}$ )  
neutrinos were captured  
in underground  
laboratories!





# Neutrino Burst of Supernova 1987A



Kamiokande-II (Japan)  
Water Cherenkov detector  
2140 tons  
Clock uncertainty  $\pm 1$  min

Irvine-Michigan-Brookhaven (US)  
Water Cherenkov detector  
6800 tons  
Clock uncertainty  $\pm 50$  ms

Baksan Scintillator Telescope  
(Soviet Union), 200 tons  
Random event cluster  $\sim 0.7$ /day  
Clock uncertainty  $+2/-54$  s

Within clock uncertainties,  
signals are contemporaneous

# Supernova Classification Scheme

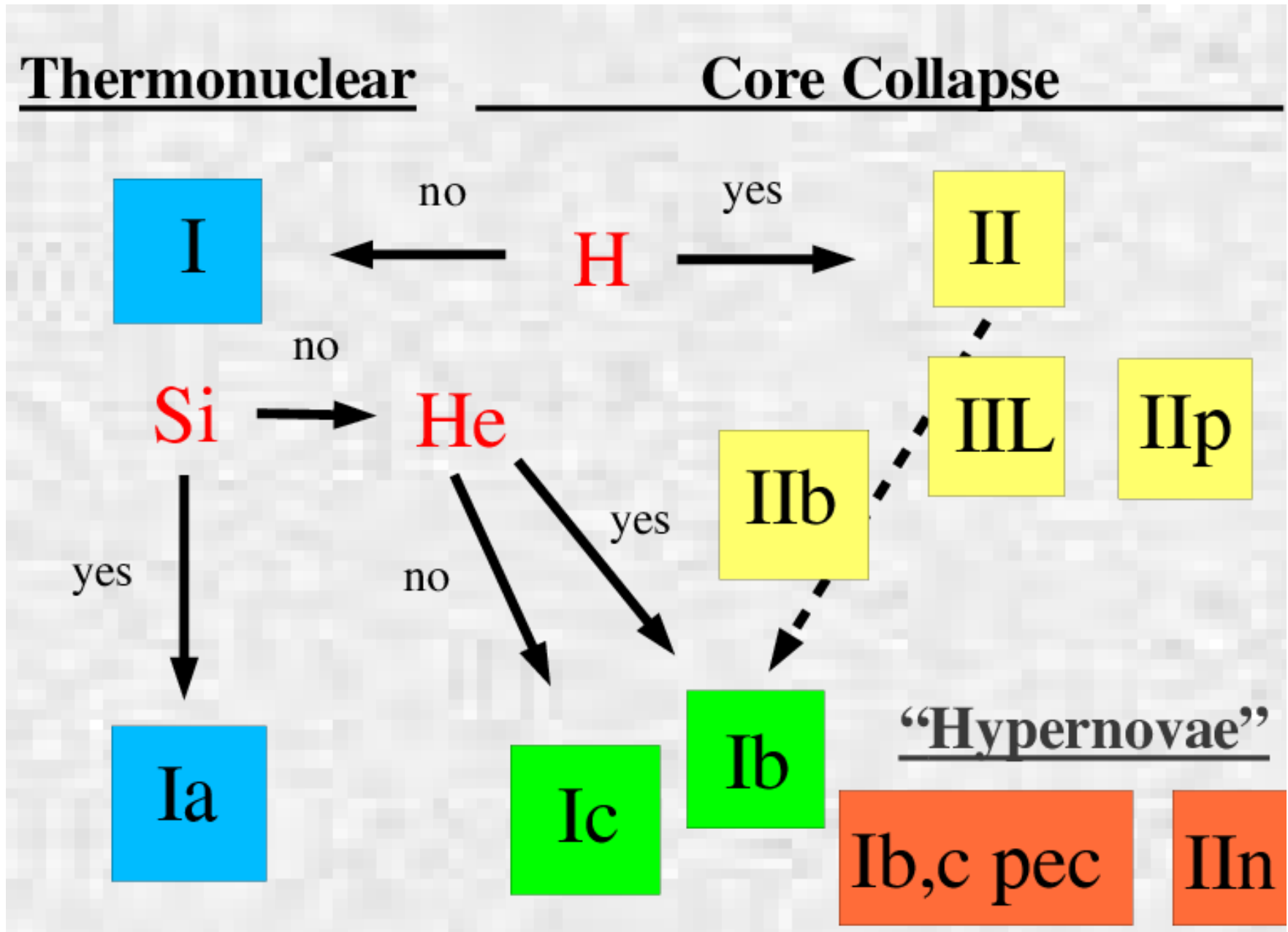
## Thermonuclear

Energy source:  
thermonuclear burning  
C, O  $\rightarrow$  Si, Ni

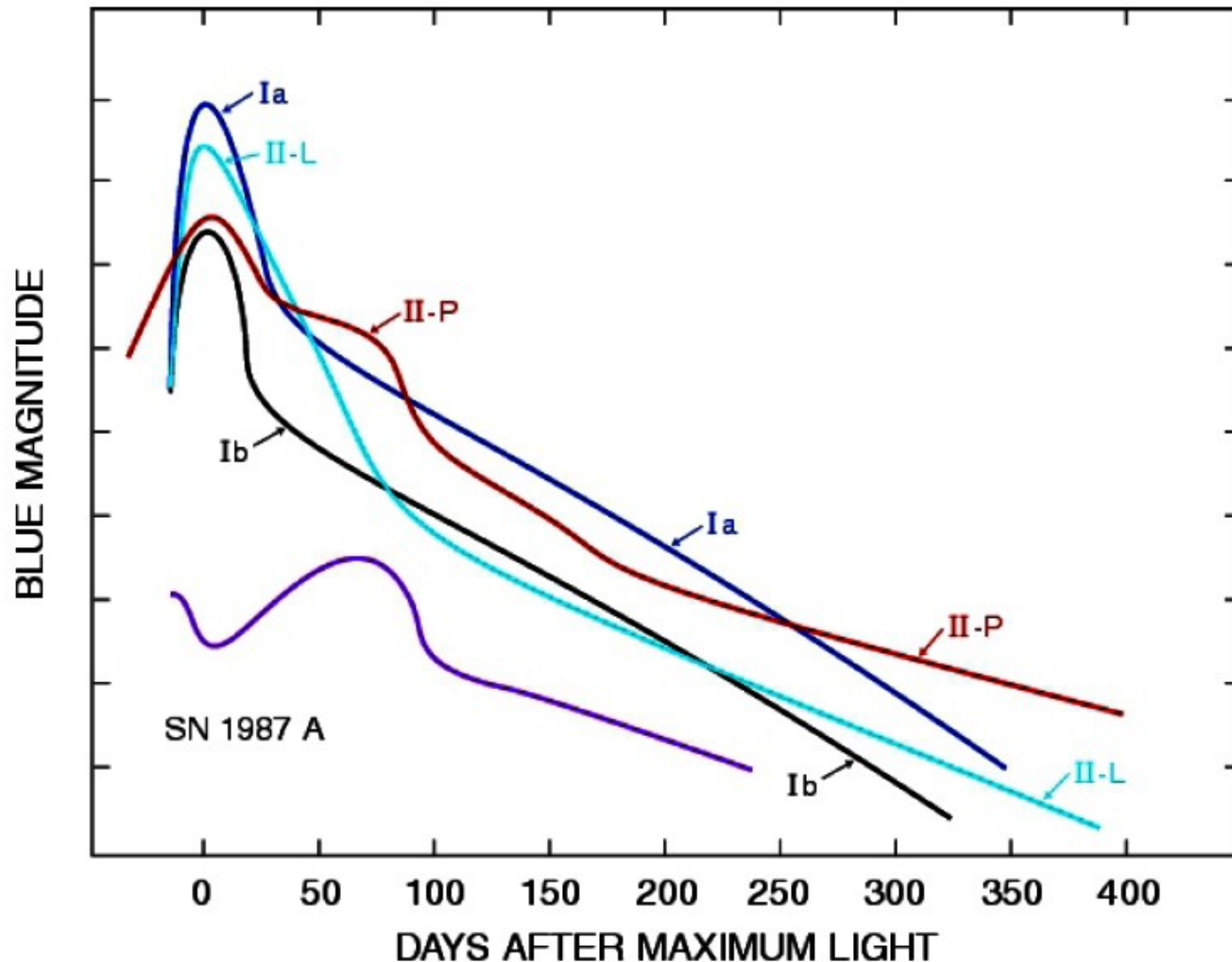
## Core Collapse

Energy source:  
gravitational binding  
energy of compact  
remnant (NS, BH)

# Supernova Classification Scheme



# Supernova Light Curves



## Supernova light curves

pronounced maximum  
after 2-3 weeks

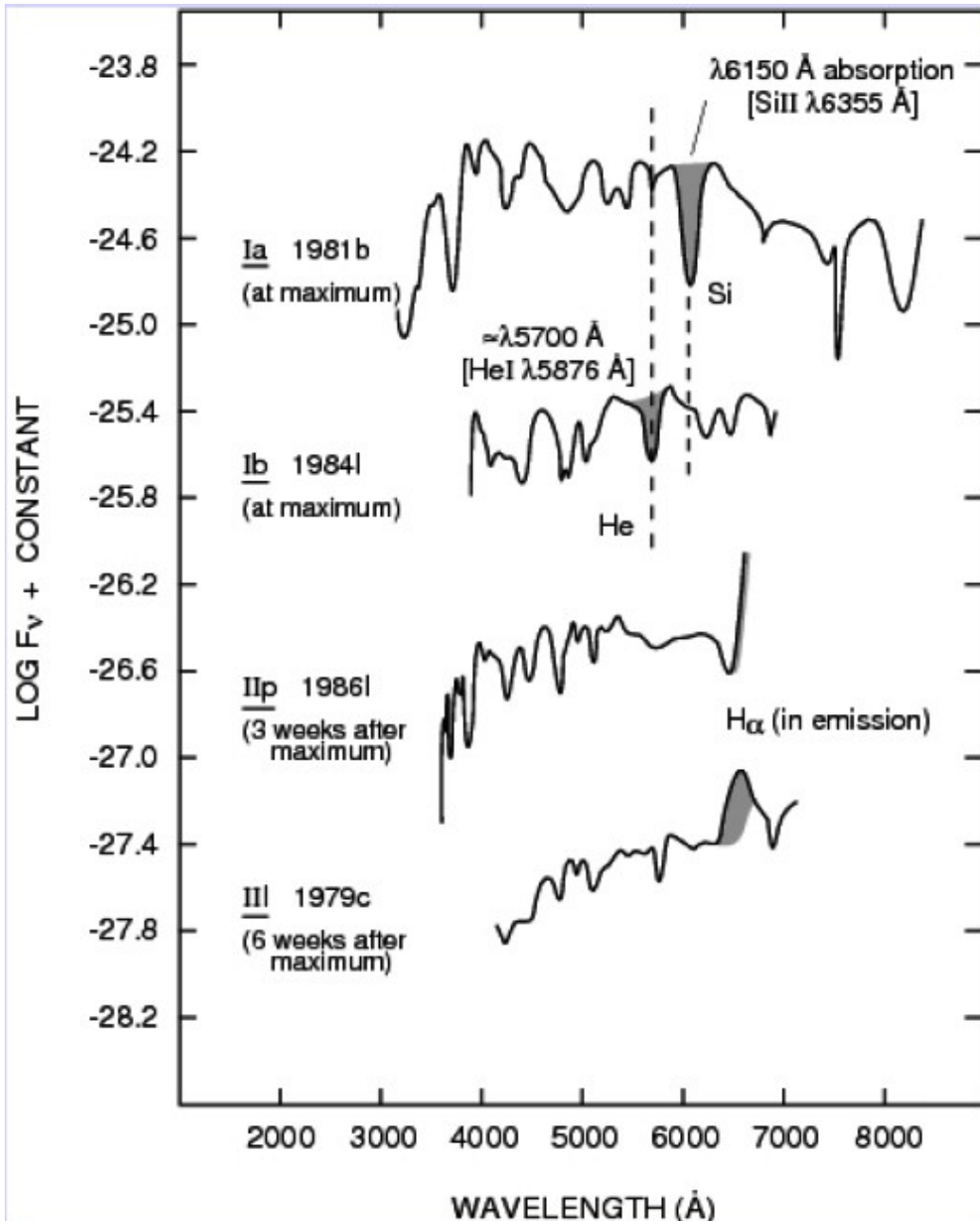
exponential tail  
(radioactive decay of  
 $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$ )

maximum brightness  
largest for SNe Ia

only SNe Ia form a (quite)  
homogeneous class  
→ standard candles!?

→ possibility to measure  
expansion of universe

# Supernova Spectra



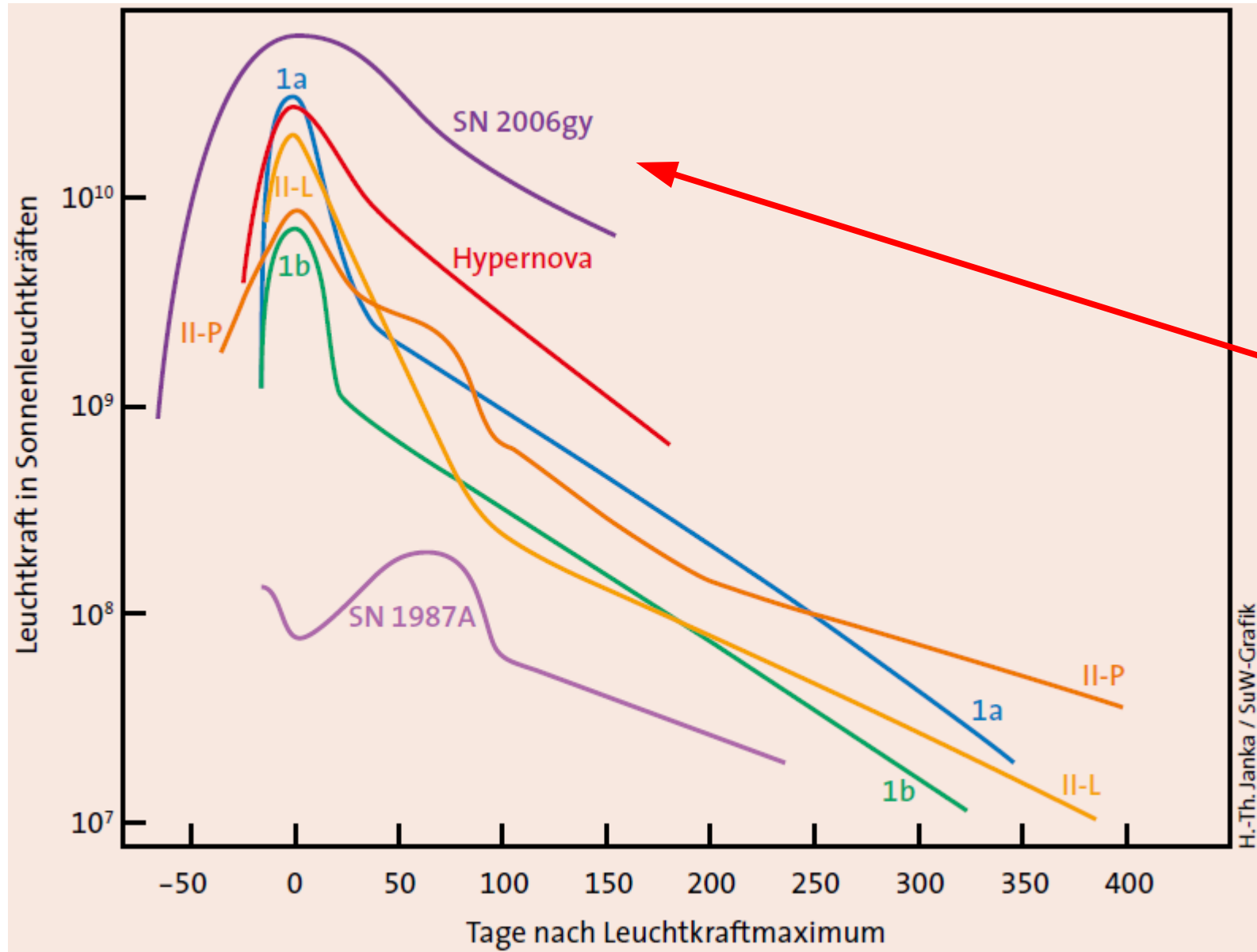
## Supernova spectra

discriminate types  
(no spectrum → no type!!)

provide information about

- stellar & explosive nucleosynthesis
- abundances and chemical stratification (tomography)
- stellar environment & progenitor star

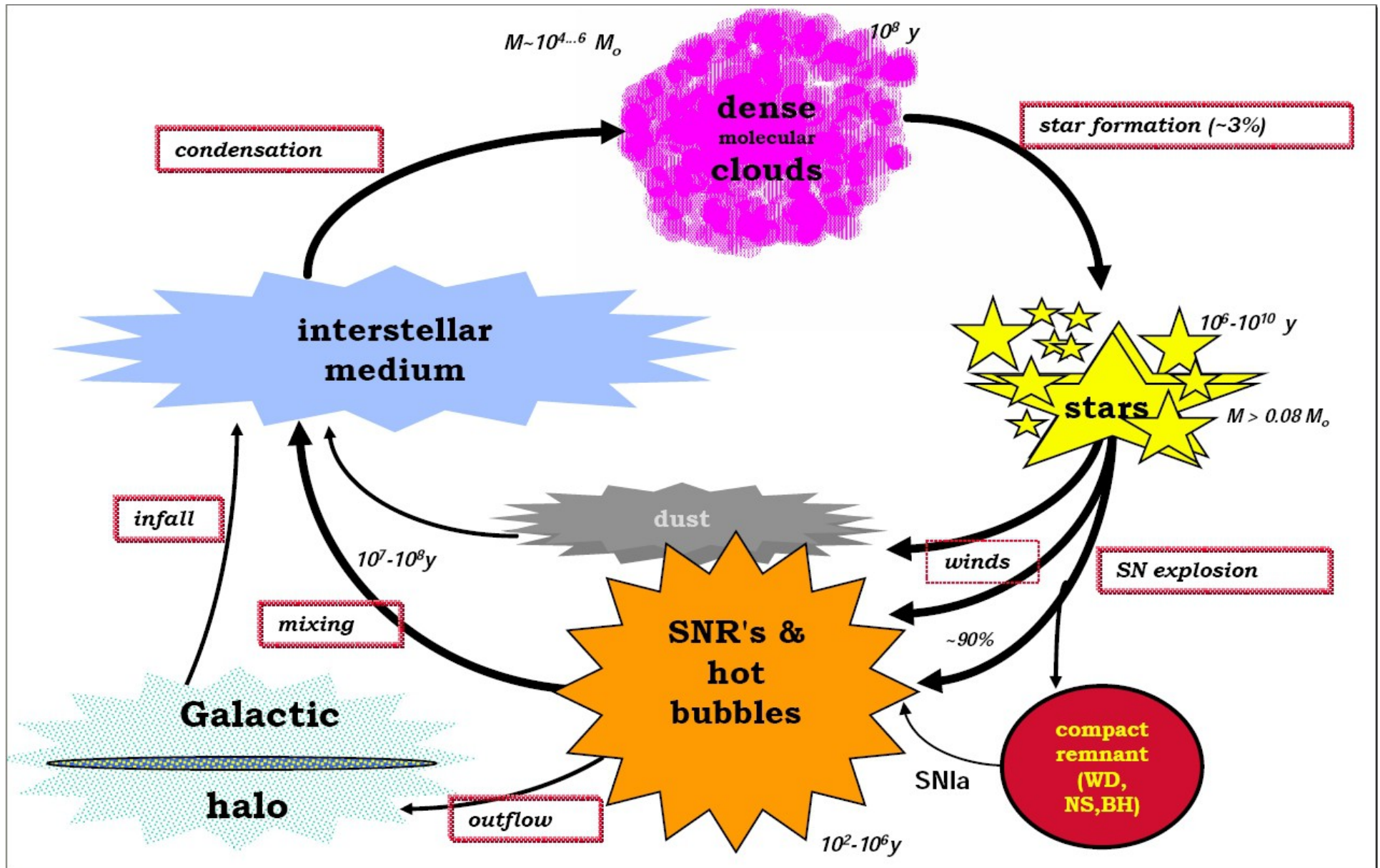
# Superluminal Supernovae



# Role of Supernovae

- strongest cosmic explosions
- sources of heavy elements
- driving force of cosmic cycle of matter
- sources of neutrinos and gravitational waves: fundamental physics
- acceleration of cosmic radiation
- birth sites of neutrons stars and black holes
- 
- 
-

# SNe in the Cosmic Cycle of Matter





# Supernova Types: Basic Differences

## Thermonuclear Supernovae (Type Ia):

Low-mass stars ( $< 8-10 M_{\text{sun}}$ )  
Highly evolved (old white dwarfs)  
Binary systems

Thermonuclear burning  
C, O  $\rightarrow$  Si, Ni

Complete destruction of star

## Core-Collapse Supernovae (Type II, Ib, Ic):

Massive stars ( $> 8-10 M_{\text{sun}}$ )  
Extended envelopes (esp. Type II)  
Single stars (binaries possible for  
Type Ib,c)

Nuclear burning by (shock)  
compression

Compact remnants are left behind:  
neutron star or black hole

# Fundamentals of Stellar Evolution

# Stellar Evolution Equations

Assumed: spherical symmetry, Newtonian gravity, single star

**Mass conservation:**

$$\frac{\partial M(r)}{\partial r} = 4\pi r^2 \rho(r) \quad (1)$$

with  $\rho$  being the mass density,  $M(r)$  the enclosed mass, and  $M(R_*) = M_*$ .

**Hydrostatic equilibrium:**

$$\rho \frac{d^2 r}{dt^2} = - \frac{\partial P(r)}{\partial r} - \frac{GM(r)\rho(r)}{r^2} = 0 \quad (2)$$

with  $P = P_{\text{gas}} + P_{\gamma}$  (+ $P_{\nu}$  +  $P_B$  +  $P_{\text{turb}}$  +  $P_{\text{deg}}$  + .....) and  $P(R_*) = 0$ .

In general:  $P = P(\rho, T, \text{composition})$ .

**Energy equation:**

$$\frac{d}{dt} \left( \frac{e}{\rho} \right) - P \frac{d}{dt} \left( \frac{1}{\rho} \right) = T \frac{ds}{dt} = \dot{\epsilon} - \frac{1}{4\pi r^2 \rho} \frac{\partial L_\gamma}{\partial r},$$

or

$$\frac{\partial}{\partial r} L_\gamma(r) = 4\pi r^2 \rho(r) \left( \dot{\epsilon} - T \frac{ds}{dt} \right) \quad (3)$$

with  $e$  being the internal energy density,  $L_\gamma$  the “luminosity”,

$\dot{\epsilon} = \dot{\epsilon}_{\text{nuc}} - \dot{\epsilon}_\nu - \dot{\epsilon}_x$ , and  $\dot{\epsilon}_{\text{grav}} \equiv -T(ds/dt)$  (“gravothermal energy source term” associated with expansion or contraction of mass).

**Total energy conservation:**

Integrate Eq. (3) over volume, using Eq. (2), to obtain for change of internal, gravitational, and nuclear energy:

$$\frac{d}{dt} (E_i + E_{\text{grav}} + E_{\text{nuc}}) = -(L_\gamma + L_\nu) \quad (3a)$$

## Energy transport:

- by radiative transfer
- by convection
- by heat conduction (irrelevant in ordinary stars)

Consider radiative transfer by diffusion for  $\lambda_{\text{mfp}} \ll h_P = |dr/d \ln P|$  (pressure scale height).

Fick's law:

$$F_\gamma = \frac{L_\gamma}{4\pi r^2} = -D \nabla e_\gamma = -\frac{1}{3} c \lambda_{\text{mfp}} \frac{\partial e_\gamma}{\partial r},$$

with  $e_\gamma = a_\gamma T^4$ ,  $\lambda_{\text{mfp}} = (\kappa \rho)^{-1}$  ( $\kappa$ : “opacity”) follows

$$\frac{\partial T}{\partial r} = -\frac{3\kappa\rho(r)L_\gamma(r)}{16\pi a_\gamma c r^2 T^3} \quad (4)$$

### Virial theorem:

Perform integration  $\int_0^{R_*} dr 4\pi r^3 [Eq. (2)]$ , using ideal gas EoS,

$$P = (\Gamma - 1)e \quad \text{with} \quad \Gamma \equiv \left( \frac{\partial \ln P}{\partial \ln \rho} \right)_s ,$$

to obtain relation between internal and gravitational energy for star in mechanical equilibrium:

$$E_{\text{grav}} = -3(\Gamma - 1)E_i . \quad (5)$$

With total energy  $E_{\text{tot}} = E_i + E_{\text{grav}}$  one gets for  $\Gamma \neq \frac{4}{3}$ :

$$E_i = -\frac{E_{\text{tot}}}{3\Gamma - 4} . \quad (5a)$$

Normal stars have  $\Gamma = \frac{5}{3}$ . When such stars lose energy,

$dE_{\text{tot}}/dt = -L$ , they become hotter (“negative specific heat”)!

# Basic Principles of Stellar Evolution

Radiating and evolving stars become hotter  
(have “negative specific heat”)

## Scaling relations:

From stellar structure equations one obtains by linearization (use  $M(r) = 0$ ,  $L_\gamma(r) = 0$  for  $r = 0$ ,  $P(R_*) = 0$ , and  $P = \bar{P}$ ,  $\rho = \bar{\rho}$ ):

$$\frac{P}{M} \sim \frac{M}{R^4}, \quad \frac{R}{M} \sim \frac{1}{R^2 \rho}, \quad \frac{T}{M} \sim \frac{L}{R^4 T^3}$$

$$\frac{L}{M} \sim \epsilon_{\text{nuc}} \sim \rho^\lambda T^\nu$$

and in particular, with the use of  $P \propto \rho T / \mu$  ( $\mu$ : mean molecular weight):

$$\frac{T^3}{\rho} \propto M^2, \quad L \propto \mu^4 M^3, \quad \tau_{\text{nuc}} \sim \frac{M}{L} \propto M^{-2}$$

with  $\tau_{\text{nuc}}$  being the nuclear burning timescale.

- **More massive stars evolve faster and live shorter!**

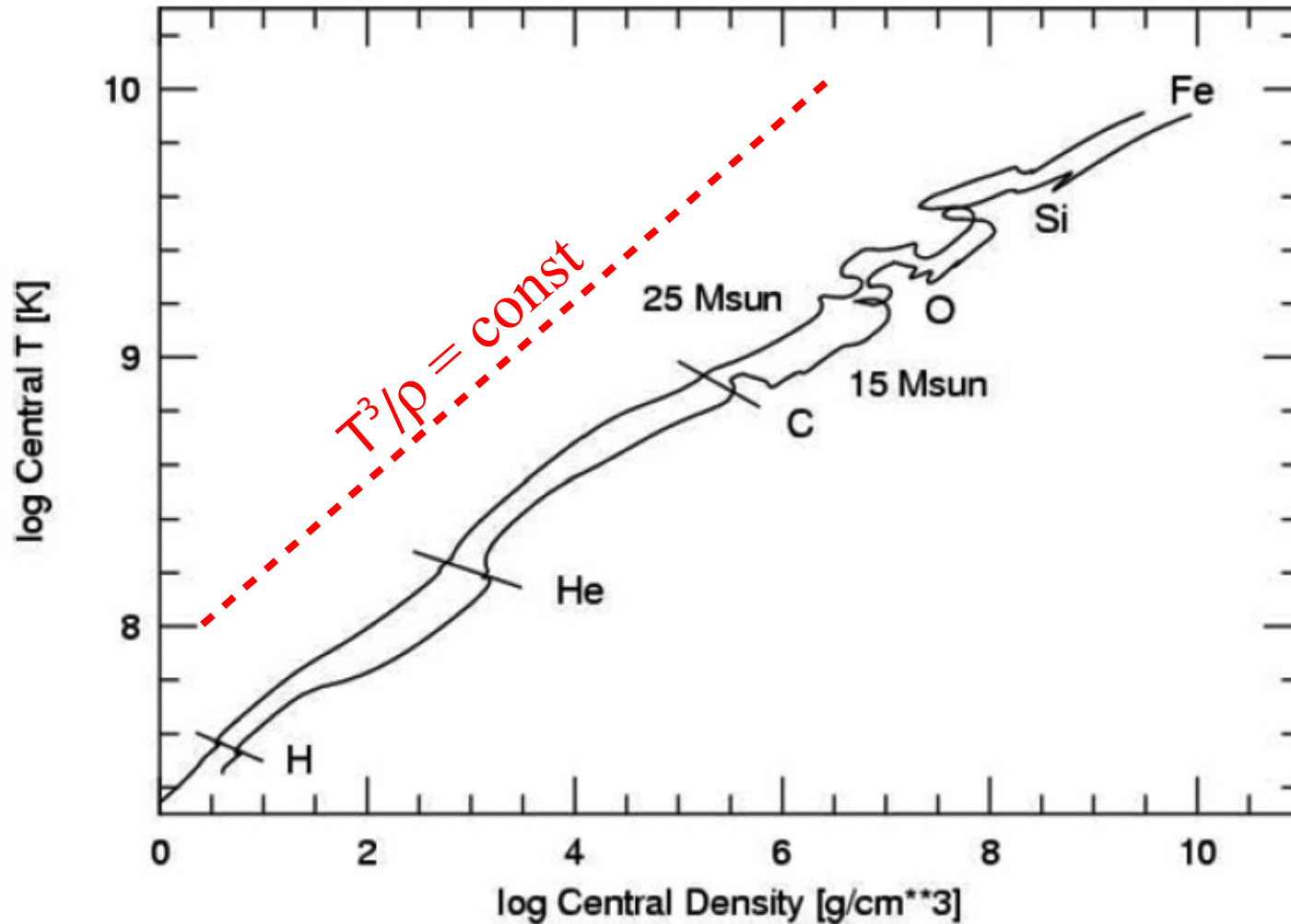


# Basic Principles of Stellar Evolution

$$T^3/\rho \sim M^2$$

- \* As star contracts and its density grows, T increases like  $\rho^{1/3}$
- \* For given density, stars with larger mass M are hotter

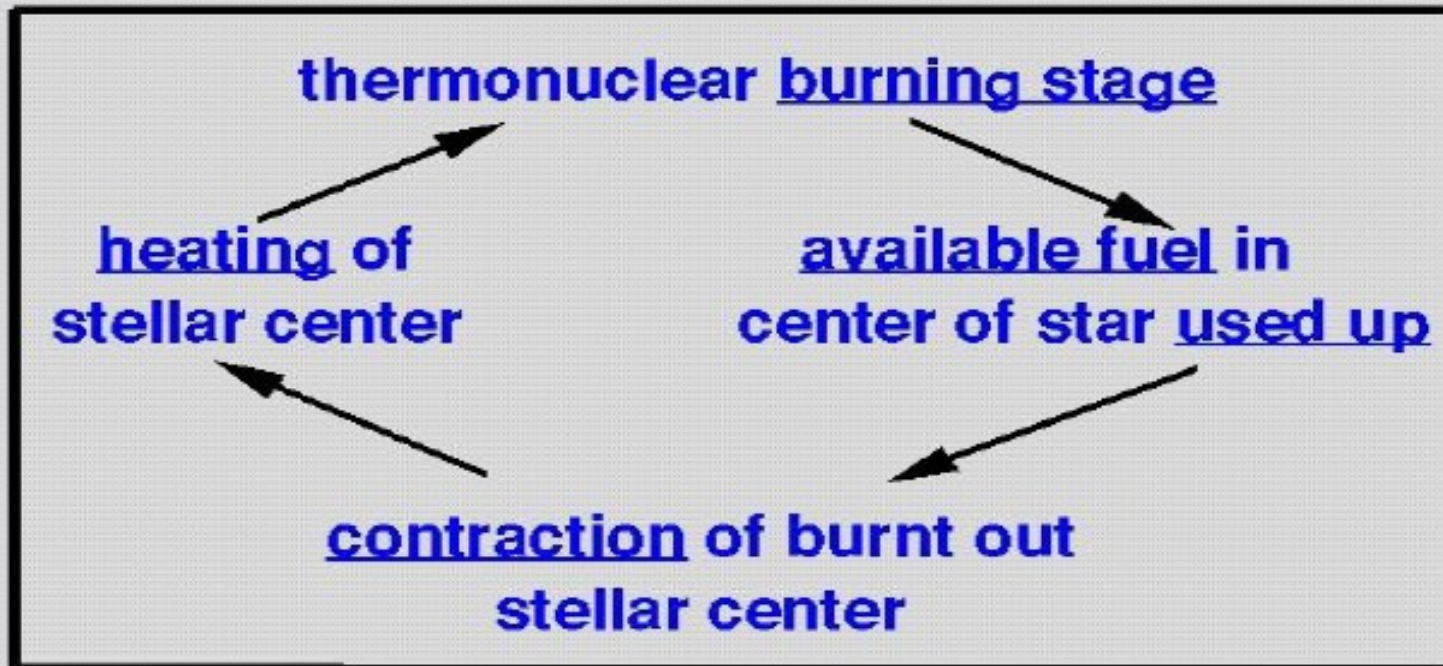
# Evolution Tracks of Massive Stars



- Central density increases roughly like 3<sup>rd</sup> power of central temperature

## Evolution towards gravitational collapse

- depending on stellar mass:  
**number of thermonuclear burning stages**



- every burning stage: **central burning + shell burning**
- stars with  **$M > 8 - 10 M_{\text{Sun}}$**  experience **all physically possible burning stages**

# Stellar Burning Stages

**Table 1 Evolution of a 15-solar-mass star.**

Stage	Timescale	Fuel or product	Ash or product	Temperature ( $10^9$ K)	Density ( $\text{gm cm}^{-3}$ )	Luminosity (solar units)	Neutrino losses (solar units)
Hydrogen	11 Myr	H	He	0.035	5.8	28,000	1,800
Helium	2.0 Myr	He	C, O	0.18	1,390	44,000	1,900
Carbon	2000 yr	C	Ne, Mg	0.81	$2.8 \times 10^5$	72,000	$3.7 \times 10^5$
Neon	0.7 yr	Ne	O, Mg	1.6	$1.2 \times 10^7$	75,000	$1.4 \times 10^8$
Oxygen	2.6 yr	O, Mg	Si, S, Ar, Ca	1.9	$8.8 \times 10^6$	75,000	$9.1 \times 10^8$
Silicon	18 d	Si, S, Ar, Ca	Fe, Ni, Cr, Ti, ...	3.3	$4.8 \times 10^7$	75,000	$1.3 \times 10^{11}$
Iron core collapse*	$\sim 1$ s	Fe, Ni, Cr, Ti, ...	Neutron star	$> 7.1$	$> 7.3 \times 10^9$	75,000	$> 3.6 \times 10^{15}$

\* The pre-supernova star is defined by the time at which the contraction speed anywhere in the iron core reaches  $1,000 \text{ km s}^{-1}$ .

# Basic Principles of Stellar Evolution

$$\tau_{\text{nuc}} \sim M^{-2}$$

More massive stars evolve faster and live shorter

# Stellar Equations of State

Grenzfall	Zustandsgleichung	ND	D
NR	$P = \frac{2}{3}\varepsilon$	$P = nk_B T$	$P \sim (Y_F \rho)^{5/3}$
ER	$P = \frac{1}{3}\varepsilon$	$P = nk_B T$ (Jüttner 1915)	$P \sim (Y_F \rho)^{4/3}$

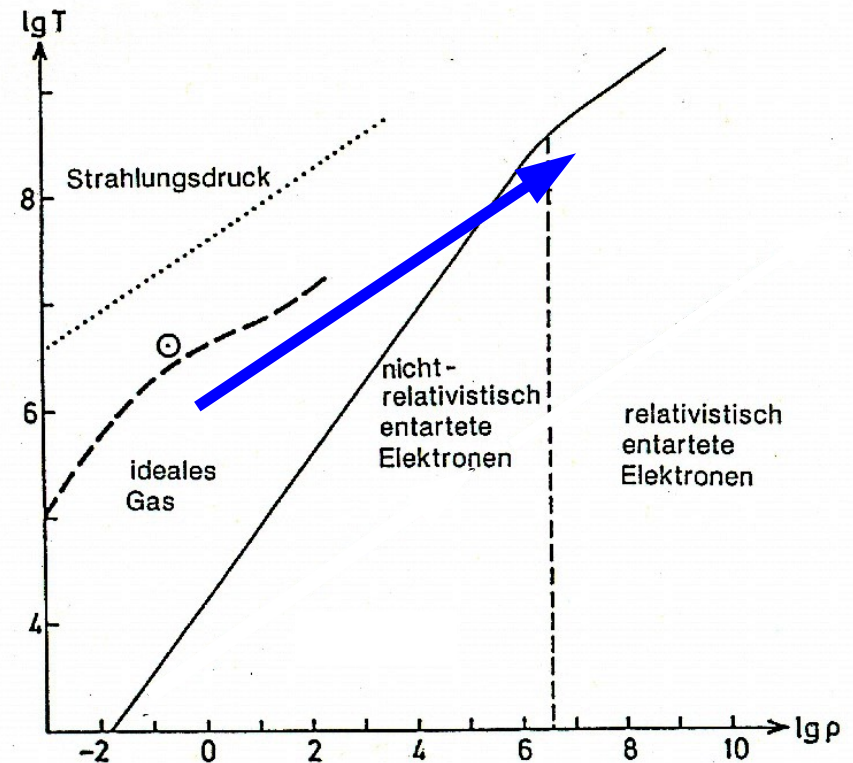
Onset of degeneracy:

$$\varepsilon_{\text{Fermi}} / kT > 1$$

- NR gas:  $\varepsilon_{\text{Fermi}} / T \sim \rho^{2/3} / T$
- ER gas:  $\varepsilon_{\text{Fermi}} / T \sim \rho^{1/3} / T$

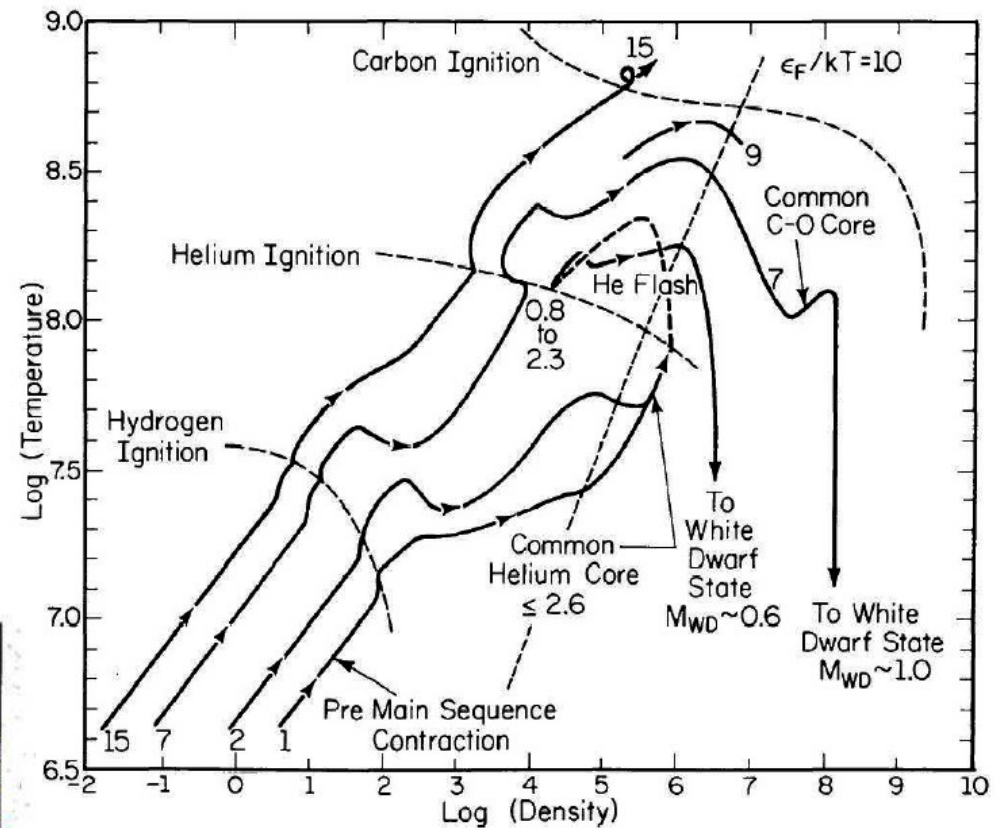
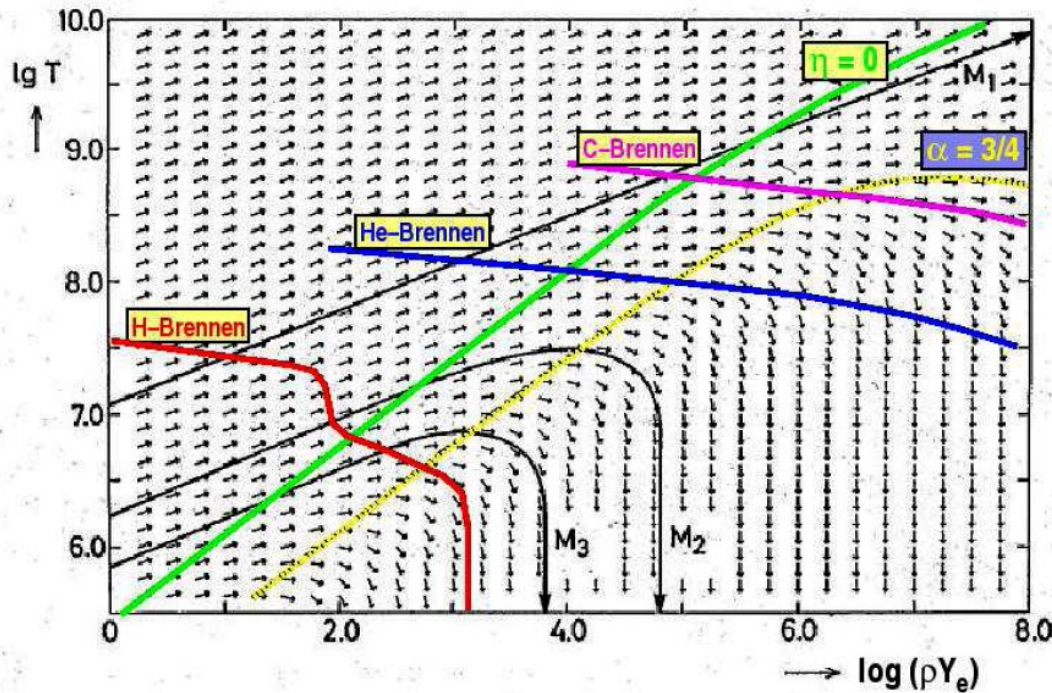
$$P = P_{\text{gas}} + P_{\text{deg}} + P_{\text{photons}}$$

- Stellar gas is in different regimes of equation of state properties as stars evolve
- Normal stars: gas behaves like **classical Boltzmann gas ( $P_{\text{gas}}$ )**
- As temperature and density rises, the stellar gas can become **degenerate and relativistic ( $P_{\text{deg}}$ )**



# Stellar Evolution towards Degeneracy

- When stellar gas becomes degenerate: further contraction does not lead to strong heating
- Stars cool at nearly fixed density
- Maximum central density and burning stage depends on stellar mass



# Stellar Evolution towards Degeneracy

Stars reach limiting burning stage and become degenerate:

$0.013 M_{\text{sun}} < M < 0.08 M_{\text{sun}}$  : deuterium burning

$0.08 M_{\text{sun}} < M < 0.5 M_{\text{sun}}$  : hydrogen burning

$0.5 M_{\text{sun}} < M < 7-8 M_{\text{sun}}$  : hydrogen and helium burning

$M < 8 M_{\text{sun}}$  : final stage of evolution is a **white dwarf**

before they reach the central carbon burning



# Chandrasekhar Mass Limit for WDs

$$M_{\text{Ch}} = 1.457(2Y_e)^2 M_{\odot}$$

## Chandrasekhar-Mass:

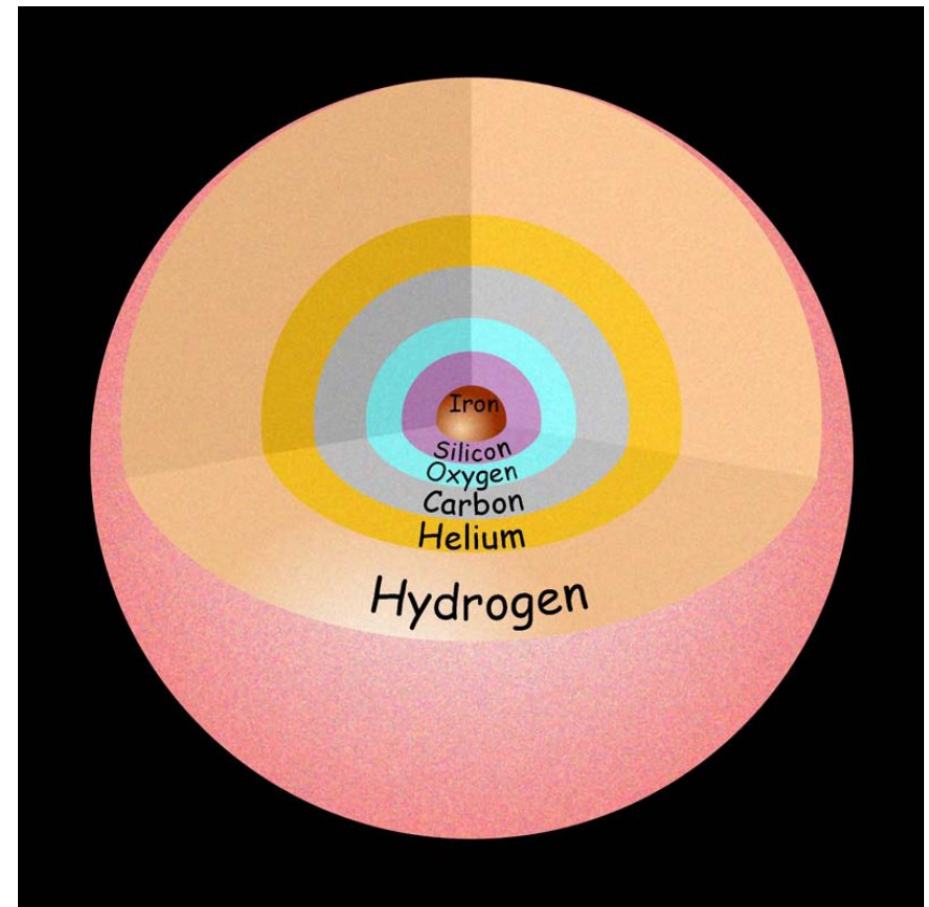
Maximum mass for a stable equilibrium of a cold star whose pressure is dominated by fully degenerate, ultrarelativistic fermions.

For  $M > M_{\text{Ch}}$  gravitational instability and collapse occurs.

# Final Stages of Stellar Evolution

- $M > 8 M_{\text{sun}}$  : stars develop **onion shell structure** before they undergo **gravitational collapse**
- $M > 10 M_{\text{sun}}$  : iron cores formed
- $M = 8-25 M_{\text{sun}}$  : **neutron star** and **supernova explosion**
- $M > 25 M_{\text{sun}}$  : **black hole** and (sometimes) **hypernova explosion**

## Onion-shell structure



# Final Stages of Stellar Evolution

- Stars with  $M_* > 8 M_{\text{sun}}$  : approach gravitational instability:  
Hydrostatic (mechanical) equilibrium breaks down  
-----> collapse of stellar core to neutron star or black hole
- Mechanical equilibrium impossible when adiabatic index of EoS

$$\Gamma_{\text{EoS}} = (\partial \ln P / \partial \ln \rho)_s < \Gamma_{\text{crit}} = 4/3 + \delta_{\text{GR}} - \delta_{\text{rot}} + \delta_{\text{vloss}}$$

(Reason: for  $\Gamma_{\text{EoS}} = (4/3 + \varepsilon)$  with  $\varepsilon < 0$  stabilizing pressure gradient increases less steeply with density than destabilizing gravitational force:

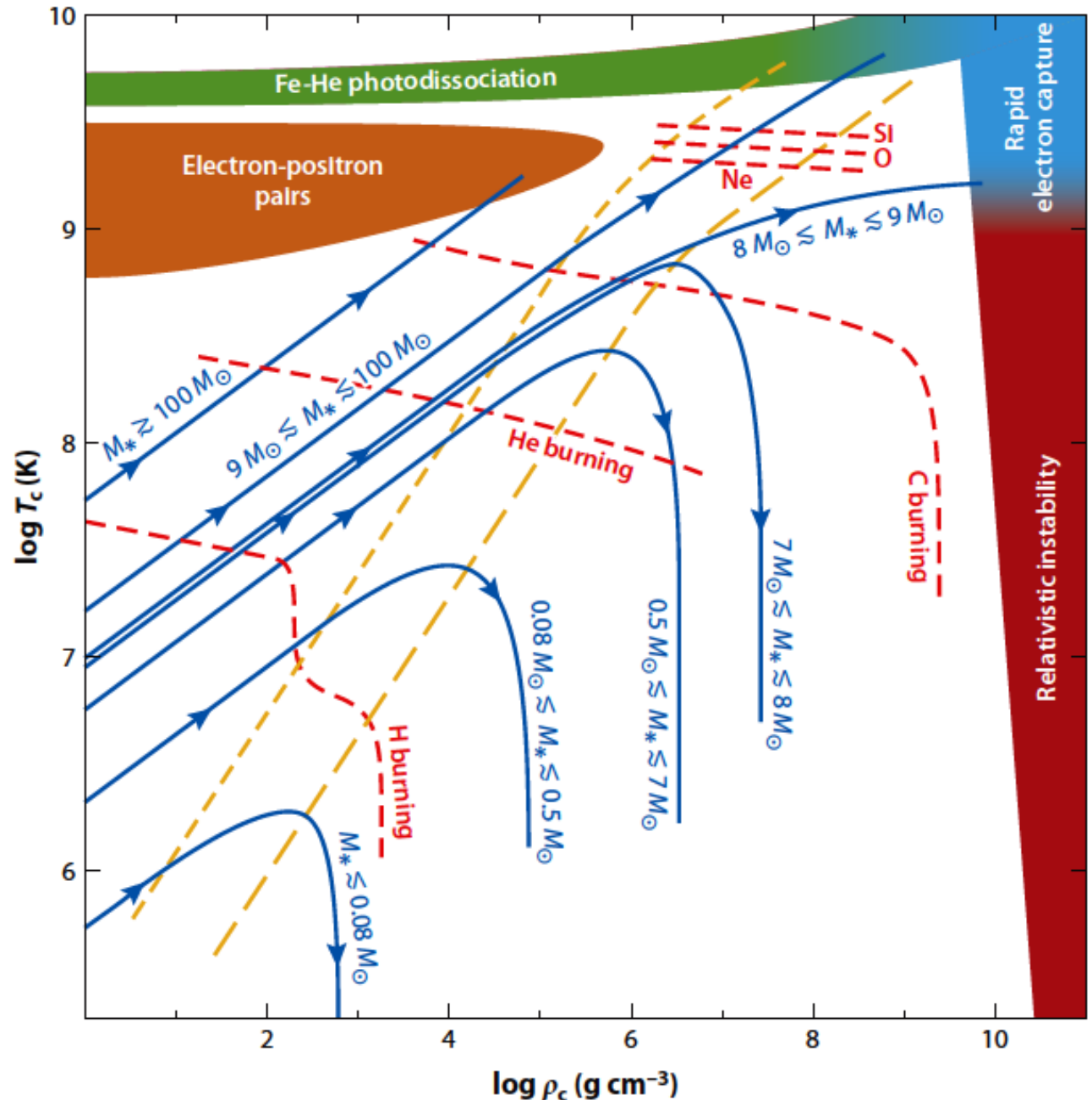
$$P/R \propto \rho^{5/3+\varepsilon} ; \quad GM/R^2 \propto \rho^{5/3}$$

# Final Stages of Massive Star Evolution

Stars with  $\sim 8-9 M_{\text{sun}}$  develop degenerate ONeMg cores  
 —> collapse by rapid e-capture

Stars with  $\sim 9-100 M_{\text{sun}}$  develop Fe cores  
 —> collapse by nuclear photodisintegration

Stars with  $> 100 M_{\text{sun}}$  approach gravitational instability before O-burning  
 —> collapse by  $e^+e^-$  pair formation

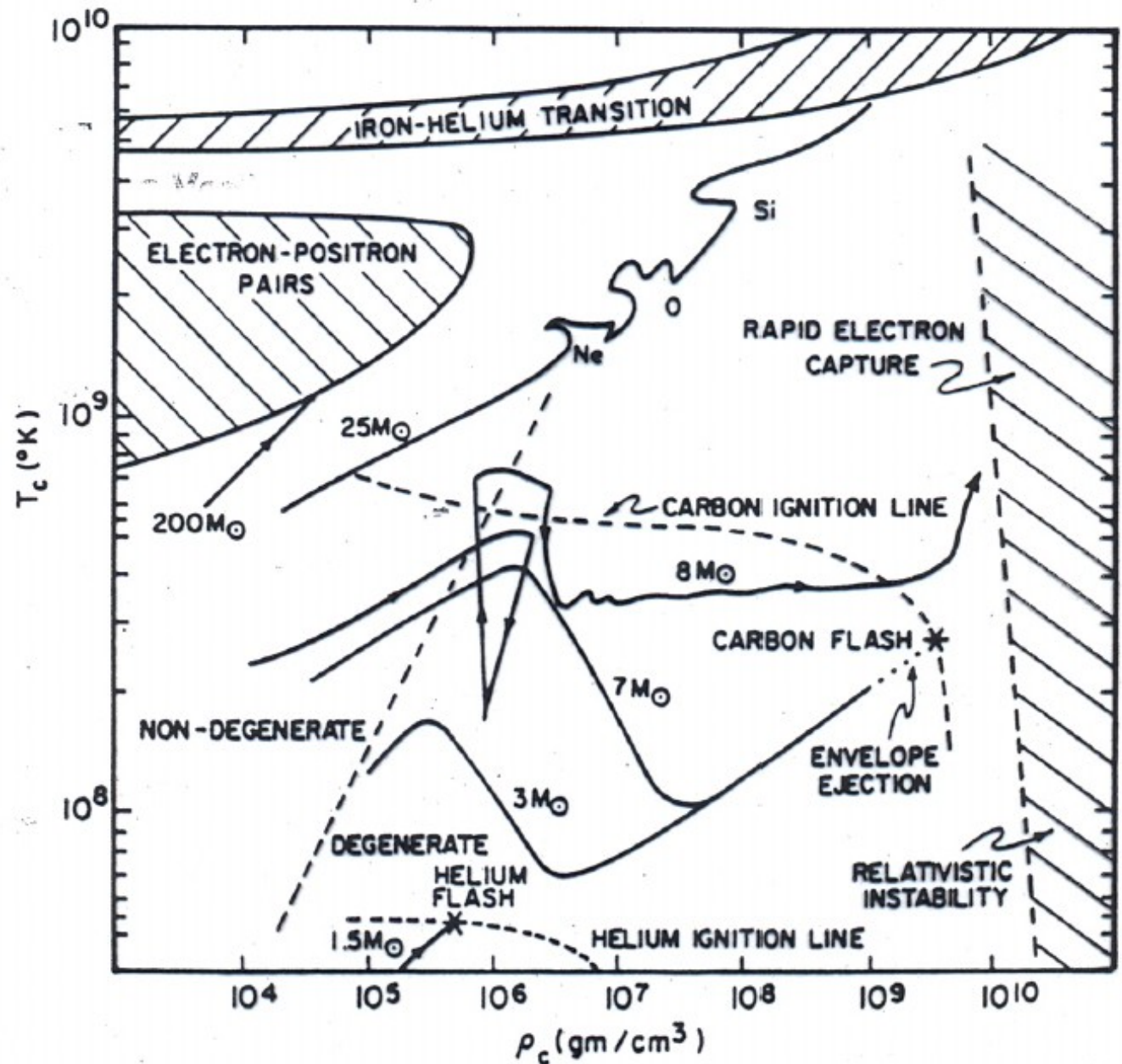


# Final Stages of Massive Star Evolution

Stars with  $\sim 8-9 M_{\text{sun}}$  develop degenerate ONeMg cores  
—> collapse by rapid e-capture

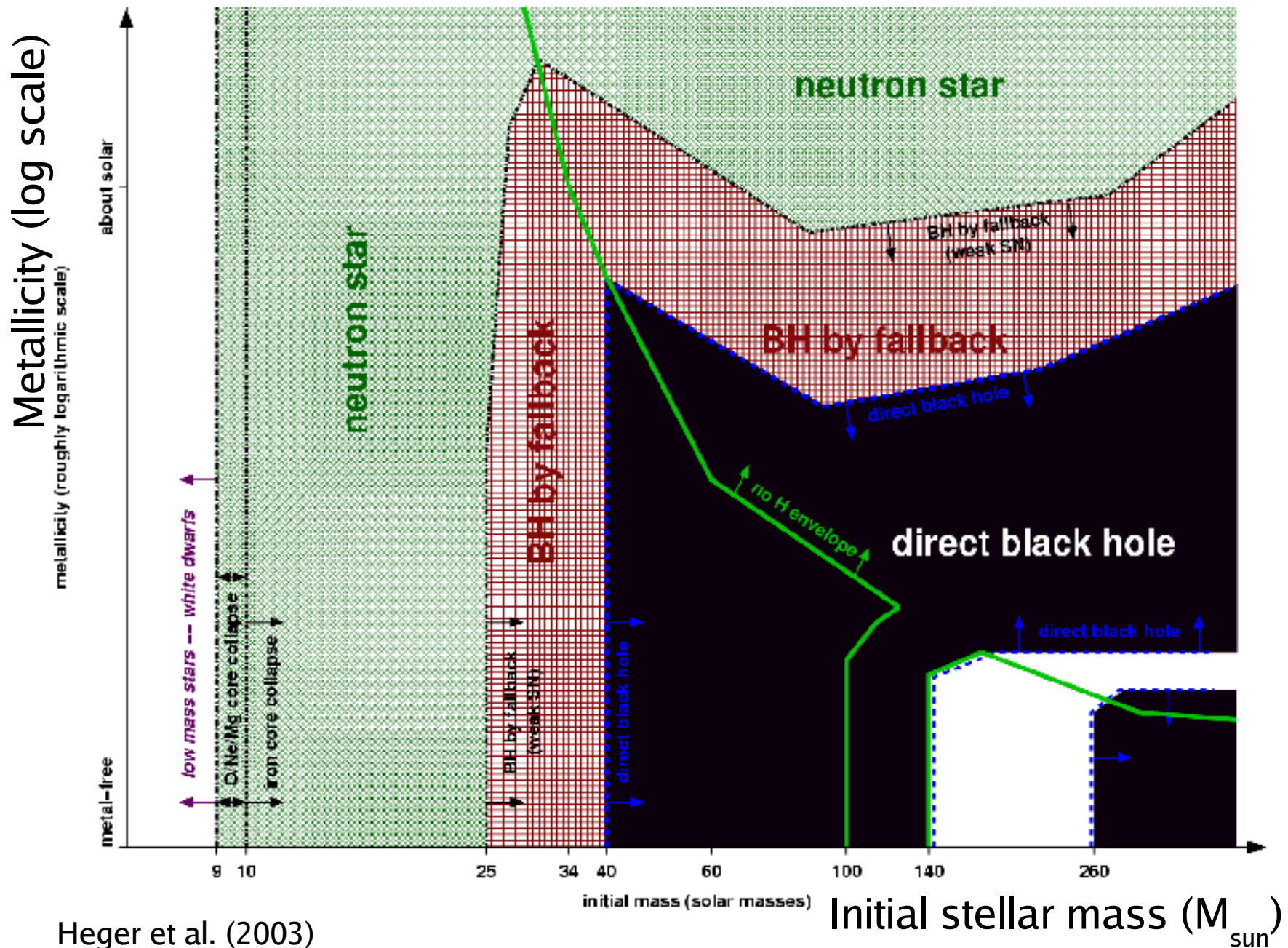
Stars with  $\sim 9-100 M_{\text{sun}}$  develop Fe cores  
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—> collapse by  $e^+e^-$  pair formation

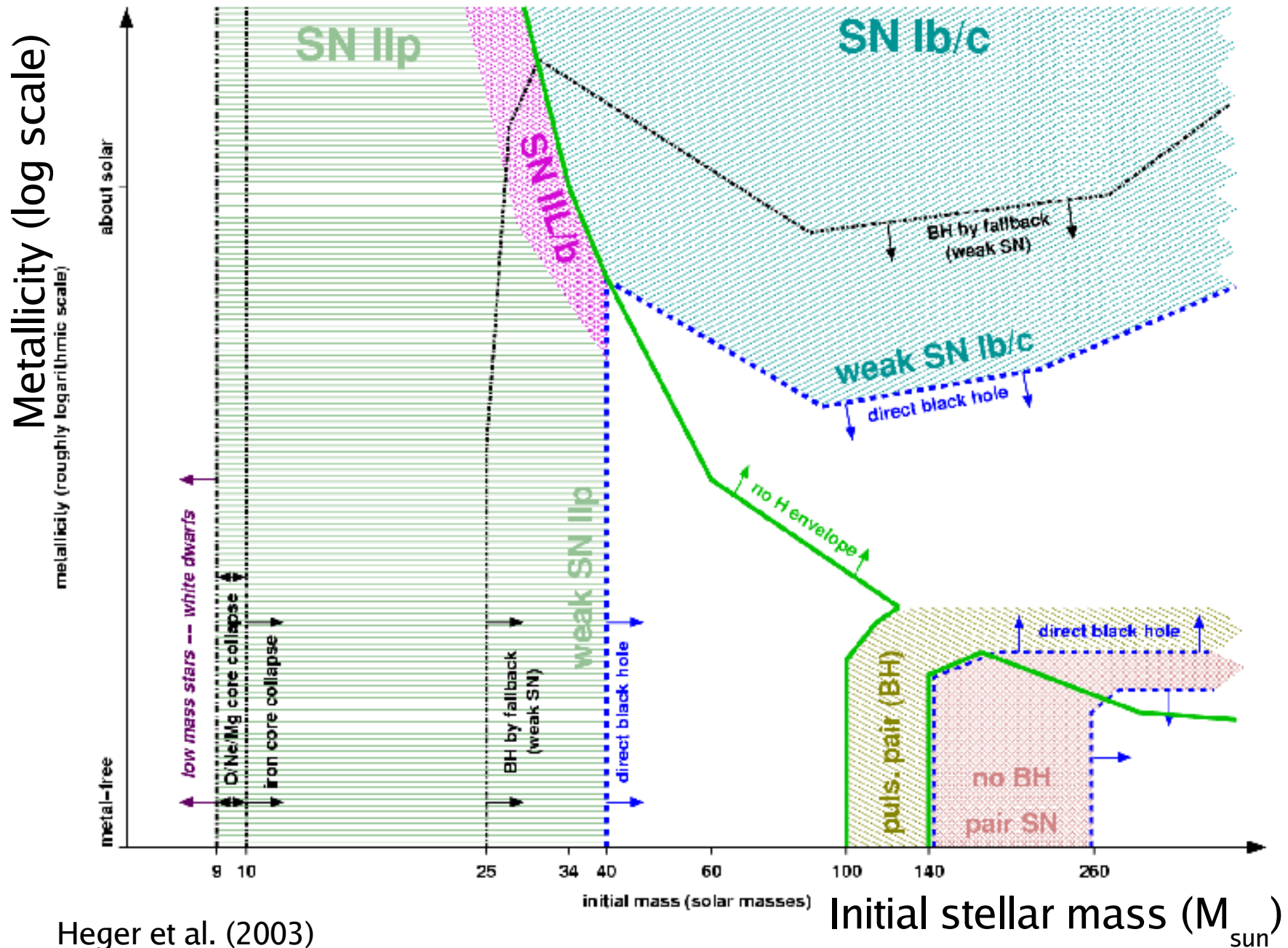


(Wheeler et al. 1990)

# Core Collapse Events and Remnants

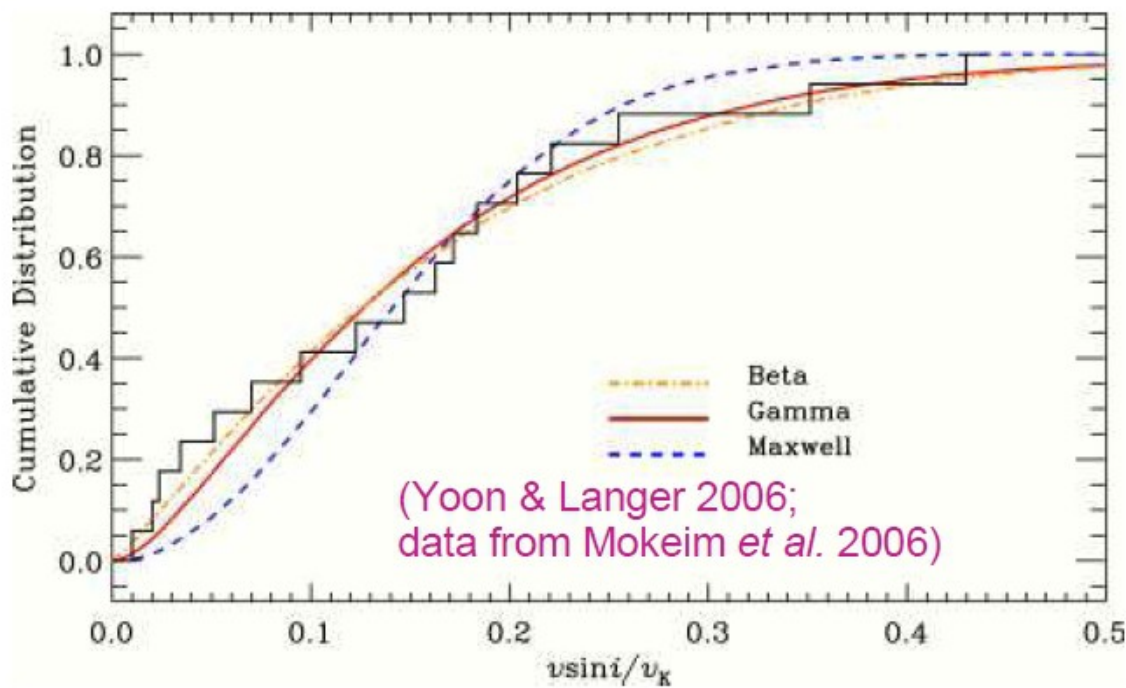


# Core Collapse Events and Remnants



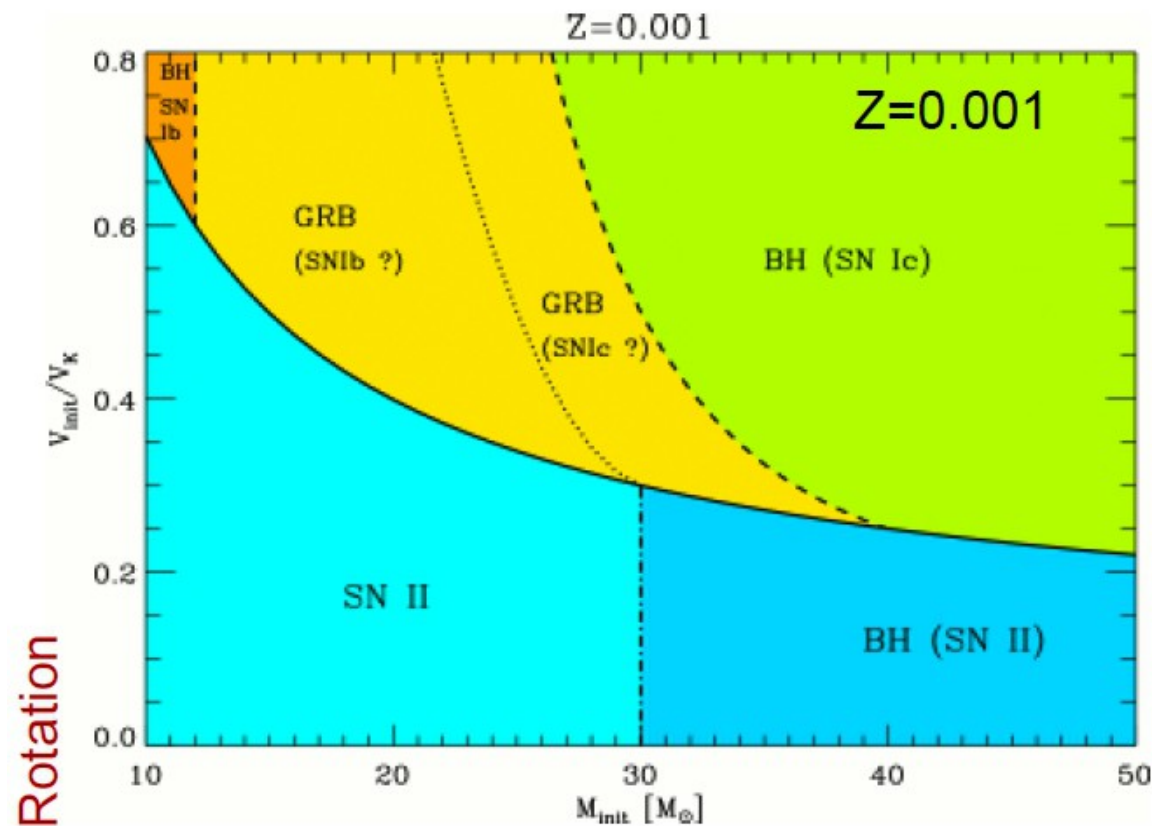
Heger et al. (2003)

# Black Holes and GRBs from Rotating Stars



A small fraction of single stars is born rotating rapidly

The fastest rotators evolve chemically homogeneously, become WR stars on the MS, and may lose less angular momentum.

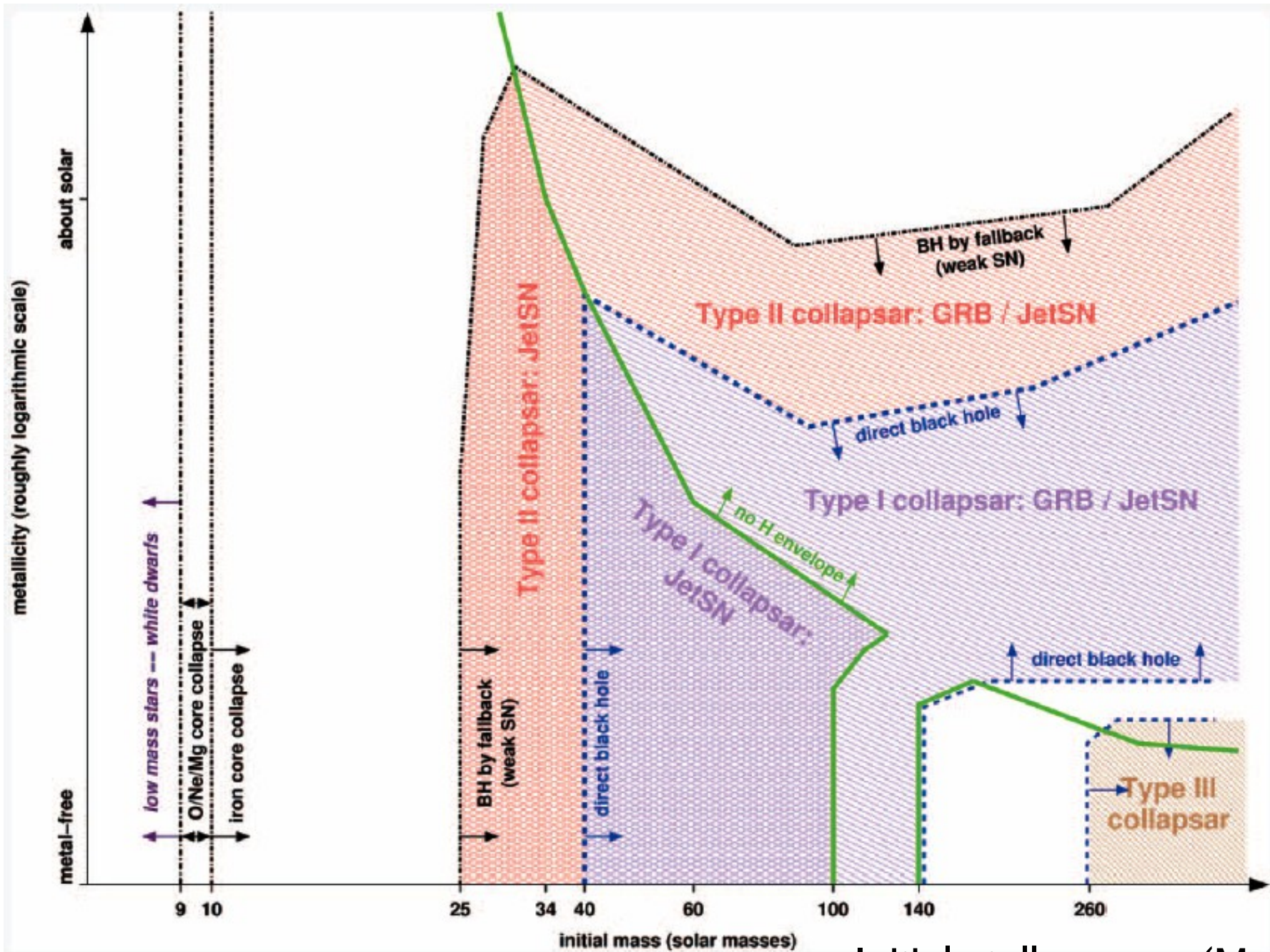


(Yoon & Langer 2006)



# Core Collapse Events and Remnants

Metallicity (log scale)

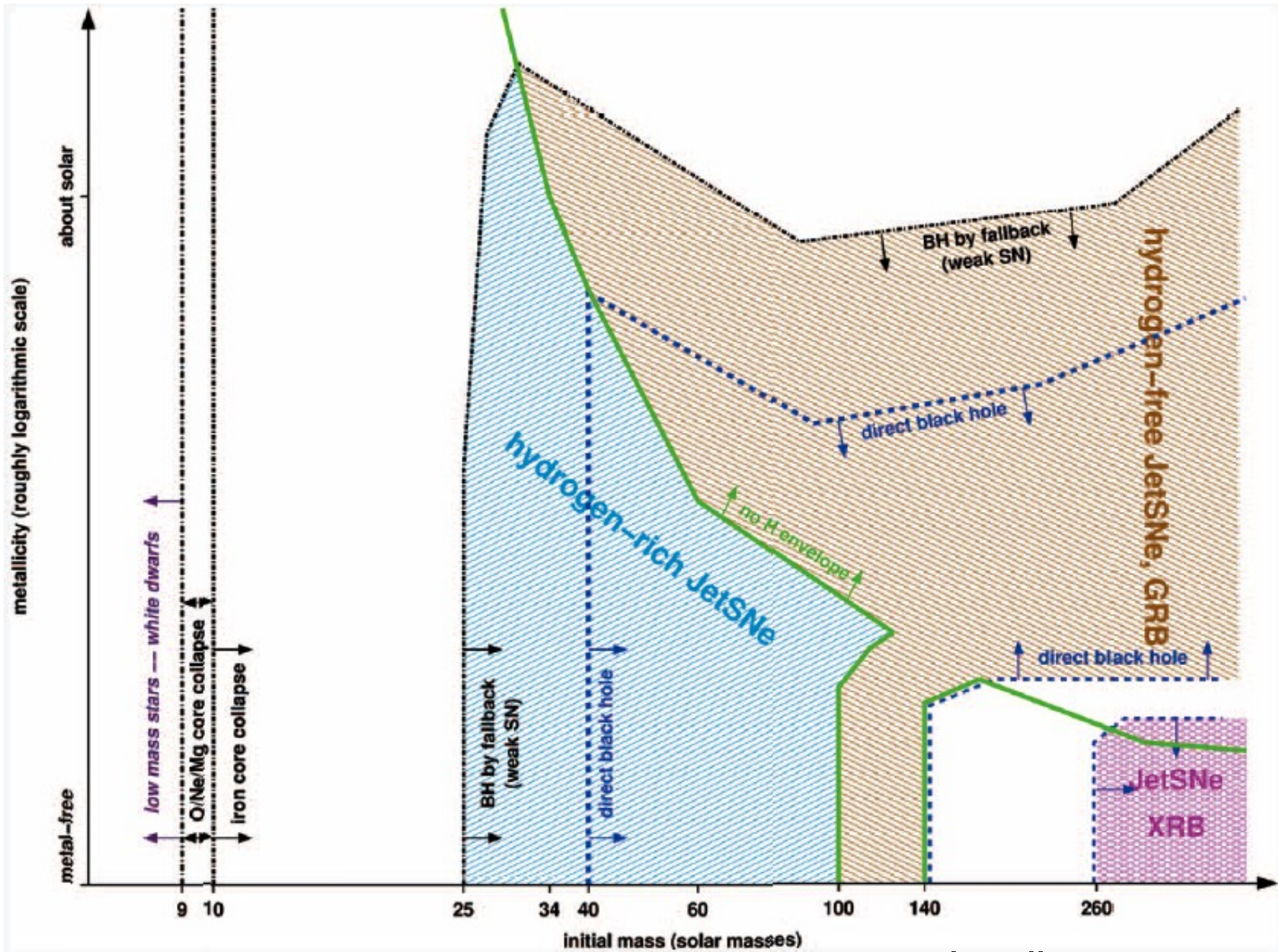


Heger et al. (2003)

Initial stellar mass ( $M_{\text{sun}}$ )

# Core Collapse Events and Remnants

Metallicity (log scale)



Heger et al. (2003)

Initial stellar mass ( $M_{\text{sun}}$ )

# Core-Collapse Events

## A heterogeneous class with growing diversity

- **Observational diversity:** Large variability due to structure of stellar mantle and envelope at time of explosion, **also on environment!**
- **Intrinsic explosion differences:** Events also differ largely in energy and Ni production <-----> **different explosions mechanisms?**
- Determining factors of stellar evolution:
  - \* **mass** of progenitor star
  - \* **“metallicity”** (i.e., heavy element abundances of stellar gas at formation)
  - \* **binary** effects
  - \* **mass loss** during stellar evolution
  - \* **stellar rotation** and **magnetic fields**
- These factors decide about:
  - \* **neutron star (NS) or black hole (BH) formation in collapse;**
  - \* **explosion mechanism, explosion energy, & Ni production;**
  - \* **lightcurve and spectral properties <—> SN classes;**
  - \* **anisotropy of explosion**

# Things that blow up

## supernovae

- CO white dwarf → Type Ia SN,  $E \approx 1B$  Bethe
- MgNeO WD, accretion → AIC, faint SN
- “SAGB” star (AGB, then SN) → EC SN
- “normal” SN (Fe core collapse) → Type II SN
- WR star (Fe CC) → Type Ib/c
- “Collapsar”, GRB → broad line Ib/a SN, “hypernova”
- Pulsational pair SN → multiple, nested Type I/II SN
- Very massive stars → pair SN,  $\lesssim 100B$  ( $1B=10^{51}$  erg)
- Very massive collapsar → IMBH, SN, hard transient
- GR He instability →  $>100 B$  SN+SMBH, or 10,000 B
- Supermassive stars →  $\gtrsim 100000 B$  SN or SMBH



1B=10<sup>51</sup> erg

MASS

A. Heger (2011)